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## A. Verilog Source Code 2001

The first and second editions of the book include Verilog using the IEEE 1364-1995 standard [340]. This third edition takes advantage of several improvements that are documented in the IEEE 1364-2001 standard, which is available for about \$100 from the IEEE bookstore [341, 342]. The Verilog 2001 improvements have now found implementations in all major design tools, [343, 344, 345] and we want to briefly review the most important new features that are used. We only review the implemented new features; for all the new features see [341].

- The entity description in the 1364-1995 standard requires that (similar to the Kernighan and Ritchie C coding) all ports appear twice, first in the port list and then in the port data-type description, e.g.,

```
module iir_pipe (x_in, y_out, clk); //----> Interface

parameter W = 14; // Bit width - 1
input      clk;
input  [W:0] x_in;   // Input
output [W:0] y_out; // Result
...
```

Note that all ports (`x_in`, `y_out`, and `clk`) are defined twice. In the 1364-2001 standard (see Sect. 12.3.4 LRM) this duplication is no longer required, i.e., the new coding is done as follows:

```
module iir_pipe      //----> Interface
#(parameter W = 14) // Bit width - 1
(input      clk,
 input  signed [W:0] x_in,   // Input
 output signed [W:0] y_out); // Result
```

- Signed data types are available in the 1364-2001 standard, which allows arithmetic signed operations to be simplified. In the signal definition line the `signed` keyword is introduced after the `input`, `output`, `reg` or `wire` keywords, e.g.,

```
reg signed [W:0] x, y;
```

Conversion between signed and unsigned type can be accomplished via the \$signed or \$unsigned conversion functions, see Sect. 4.5 LRM. For signed constants we introduce a small s or capital S between the hyphen and the base, e.g., 'sd90 for a signed constant 90. Signed arithmetic operations can be done using the conventional divide / or multiply \* operators. For power-of-2 factors we can use the new arithmetic left <<< or right shift >>> operations, see Sect. 4.1.23 LRM. Note the three shift operations symbols used to distinguish the unsigned shifts that use two shift symbols. Signed or zero extension is automatically done depending on the data type. From the IIR filter examples we can now replace the old-style operation:

```
...
y <= x + {y[W],y[W:1]} + {{2{y[W]}},y[W:2]};  
...                                // i.e., x + y / 2 + y / 4;
```

with the 1364-2001 Verilog style operations using the divide operator:

```
y <= x + y / 'sd2 + y / 'sd4; // div with / uses 92 LEs.
```

Note the definition as signed divide for the constants, the code

```
y <= x + y / 2 + y / 4;
```

will show incorrect simulation results in Quartus II in versions 4.0, 4.2, 5.0, 5.1 but works fine in our web edition 6.0. Alternatively we can use the arithmetic right shift operator to implement the divide by power-of-2 values.

```
y <= x + (y >>> 1) + (y >>> 2); // div with >>> uses 60 LEs
```

It is evident that this notation makes the arithmetic operation much more readable than the old-style coding. Although both operations are functional equivalent, the Quartus synthesis results reveals that the divide is mapped to a different architecture and needs therefore more LEs (92 compared with 60 LEs) than used by the arithmetic shift operations. From the comparison to the VHDL synthesis data we conclude that 60 LEs is the expect result. This is the reason we will use the arithmetic left and right shift throughout the examples.

- The implicit event\_expression list allows one to add automatically all right-hand-side variables to be added to the event expression, i.e., from the bproc examples

```
...
always @(Are or Bre or Aim or Bim)
begin
...

```

we now simply use

```

...
    always @(*)
    begin
    ...

```

This reduces essentially the RTL simulation errors due to missing variables in the event listing, see Sect. 9.7.5 LRM for details.

- The **generate** statement introduced in the 1364-2001 Verilog standard allows one to instantiate several components using a single generate loop construct. The LRM Sects. 12.1.3.2-4 show eight different generate examples. We use the generate in the **fir\_gen**, **fir\_lms**, and **fir6dlms** files. Note that you also need to define a **genvar** as a loop variable used for the generate statement, see Sect. 12.1.3.1 LRM for details.

The 1364-2001 Verilog standard introduces 21 new keywords. We use the new keywords **endgenerate**, **generate**, **genvar**, **signed**, and **unsigned**. We have not used the new keywords:

```

automatic, cell, config, design, endconfig, incdir, include,
instance, liblist, library, localparam, noshowcancelled,
pulsestyle_onevent, pulsestyle_onedetect, showcancelled, use

```

The next pages contain the Verilog 1364-2001 code of all design examples. The old style Verilog 1364-1995 code can be found in [57]. The synthesis results for the examples are listed on page 731.

```

//*****
// IEEE STD 1364-2001 Verilog file: example.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
//`include "220model.v" // Using predefined components

module example //----> Interface
  #(parameter WIDTH =8) // Bit width
  (input clk,
   input [WIDTH-1:0] a, b, op1,
   output [WIDTH-1:0] sum, d);

  wire [WIDTH-1:0] c;           // Auxiliary variables
  reg  [WIDTH-1:0] s;           // Infer FF with always
  wire [WIDTH-1:0] op2, op3;

  wire clkena, ADD, ena, aset, sclr, sset, aload, sload,
        aclr, ovf1, cin1; // Auxiliary lpm signals

// Default for add:
  assign cin1=0; assign aclr=0; assign ADD=1;

```

```

assign ena=1; assign aclr=0; assign aset=0;
assign sclr=0; assign sset=0; assign aload=0;
assign sload=0; assign clkena=0; // Default for FF

assign op2 = b;           // Only one vector type in Verilog;
                         // no conversion int -> logic vector necessary

// Note when using 220model.v ALL component's signals
// must be defined, default values can only be used for
// the parameters.

lpm_add_sub add1          //----> Component instantiation
( .result(op3), .dataa(op1), .datab(op2)); // Used ports
// .cin(cin1),.cout(cr1), .add_sub(ADD), .clken(clkena),
// .clock(clk), .overflow(ovl1), .aclr(aclr)); // Unused
defparam add1.lpm_width = WIDTH;
defparam add1.lpm_representation = "SIGNED";

lpm_ff reg1
( .data(op3), .q(sum), .clock(clk)); // Used ports
// .enable(ena), .aclr(aclr), .aset(aset), .sclr(sclr),
// .sset(sset), .aload(aload), .sload(sload)); // Unused
defparam reg1.lpm_width = WIDTH;

assign c = a + b; //----> Continuous assignment statement

always @(posedge clk) //----> Behavioral style
begin : p1           // Infer register
    s = c + s;        // Signal assignment statement
end
assign d = s;

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: fun_text.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// A 32-bit function generator using accumulator and ROM
//'include "220model.v"

module fun_text           //----> Interface
#(parameter WIDTH = 32)   // Bit width
(input                  clk,

```

```

input  [WIDTH-1:0]  M,
output [7:0]  sin, acc);

wire [WIDTH-1:0] s, acc32;
wire [7:0] msbs;           // Auxiliary vectors
wire ADD, ena, asset, sclr, sset; // Auxiliary signals
wire aload, sload, aclr, ovf1, cin1, clkena;

// Default for add:
assign clkena=0; assign cin1=0; assign ADD=1;
//default for FF:
assign ena=1; assign aclr=0; assign asset=0;
assign sclr=0; assign sset=0; assign aload=0;
assign sload=0;

lpm_add_sub add_1           // Add M to acc32
( .result(s), .dataaa(acc32), .dataab(M)); // Used ports
// .cout(cr1), .add_sub(ADD), .overflow(ovl1), // Unused
// .clock(clk),.cin(cin1), .clken(clkena), .aclr(aclr));
//
defparam add_1.lpm_width = WIDTH;
defparam add_1.lpm_representation = "UNSIGNED";

lpm_ff reg_1           // Save accu
( .data(s), .q(acc32), .clock(clk)); // Used ports
// .enable(ena), .aclr(aclr), .asset(asset), // Unused ports
// .sset(sset), .aload(aload), .sload(sload),.sclr(sclr));
defparam reg_1.lpm_width = WIDTH;

assign msbs = acc32[WIDTH-1:WIDTH-8];
assign acc = msbs;

lpm_rom rom1
( .q(sin), .inclock(clk), .outclock(clk),
  .address(msbs)); // Used ports
// .memenab(ena) ; // Unused port
defparam rom1.lpm_width = 8;
defparam rom1.lpm_widthhad = 8;
defparam rom1.lpm_file = "sine.mif";

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: cmul7p8.v

```

```

// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module cmul7p8                                // -----> Interface
    (input  signed [4:0] x,
     output signed [4:0] y0, y1, y2, y3);

    assign y0 = 7 * x / 8;
    assign y1 = x / 8 * 7;
    assign y2 = x/2 + x/4 + x/8;
    assign y3 = x - x/8;

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: add1p.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
//`include "220model.v"

module add1p
#(parameter WIDTH    = 19, // Total bit width
         WIDTH1   = 9,  // Bit width of LSBs
         WIDTH2   = 10) // Bit width of MSBs
    (input  [WIDTH-1:0] x, y, // Inputs
     output [WIDTH-1:0] sum, // Result
     input      clk, // Clock
     output      LSBs_Carry); // Test port

    reg [WIDTH1-1:0] l1, l2, s1; // LSBs of inputs
    reg [WIDTH1:0] r1;           // LSBs of inputs
    reg [WIDTH2-1:0] l3, l4, r2, s2; // MSBs of input

    always @(posedge clk) begin
        // Split in MSBs and LSBs and store in registers
        // Split LSBs from input x,y
        l1[WIDTH1-1:0] <= x[WIDTH1-1:0];
        l2[WIDTH1-1:0] <= y[WIDTH1-1:0];
        // Split MSBs from input x,y
        l3[WIDTH2-1:0] <= x[WIDTH2-1+WIDTH1:WIDTH1];
        l4[WIDTH2-1:0] <= y[WIDTH2-1+WIDTH1:WIDTH1];
    //***** First stage of the adder *****/
        r1 <= {1'b0, l1} + {1'b0, l2};
        r2 <= l3 + l4;
    //***** Second stage of the adder *****/
        s1 <= r1[WIDTH1-1:0];

```

```

// Add MSBs (x+y) and carry from LSBs
    s2 <= r1[WIDTH1] + r2;
end

assign LSBs_Carry = r1[WIDTH1]; // Add a test signal

// Build a single output word of WIDTH = WIDTH1 + WIDTH2
assign sum = {s2, s1};

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: add2p.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// 22-bit adder with two pipeline stages
// uses no components

//`include "220model.v"

module add2p
#(parameter WIDTH    = 28,      // Total bit width
        WIDTH1   = 9,       // Bit width of LSBs
        WIDTH2   = 9,       // Bit width of middle
        WIDTH12  = 18,     // Sum WIDTH1+WIDTH2
        WIDTH3   = 10)     // Bit width of MSBs
(input  [WIDTH-1:0] x, y,      // Inputs
 output [WIDTH-1:0] sum,       // Result
 output LSBs_Carry, MSBs_Carry, // Single bits
 input   clk);                // Clock

reg [WIDTH1-1:0] l1, l2, v1, s1; // LSBs of inputs
reg [WIDTH1:0]   q1;           // LSBs of inputs
reg [WIDTH2-1:0] l3, l4, s2;   // Middle bits
reg [WIDTH2:0]   q2, v2;       // Middle bits
reg [WIDTH3-1:0] l5, l6, q3, v3, s3; // MSBs of input

// Split in MSBs and LSBs and store in registers
always @ (posedge clk) begin
    // Split LSBs from input x,y
    l1[WIDTH1-1:0] <= x[WIDTH1-1:0];
    l2[WIDTH1-1:0] <= y[WIDTH1-1:0];
    // Split middle bits from input x,y
    l3[WIDTH2-1:0] <= x[WIDTH2-1+WIDTH1:WIDTH1];
    l4[WIDTH2-1:0] <= y[WIDTH2-1+WIDTH1:WIDTH1];

```

```

// Split MSBs from input x,y
15[WIDTH3-1:0] <= x[WIDTH3-1+WIDTH12:WIDTH12];
16[WIDTH3-1:0] <= y[WIDTH3-1+WIDTH12:WIDTH12];
//***** First stage of the adder *****
q1 <= {1'b0, 11} + {1'b0, 12}; // Add LSBs of x and y
q2 <= {1'b0, 13} + {1'b0, 14}; // Add LSBs of x and y
q3 <= 15 + 16; // Add MSBs of x and y
//***** Second stage of the adder *****
v1 <= q1[WIDTH1-1:0]; // Save q1
// Add result from middle bits (x+y) and carry from LSBs
v2 <= q1[WIDTH1] + {1'b0,q2[WIDTH2-1:0]};
// Add result from MSBs bits (x+y) and carry from middle
v3 <= q2[WIDTH2] + q3;
//***** Third stage of the adder *****
s1 <= v1; // Save v1
s2 <= v2[WIDTH2-1:0]; // Save v2
// Add result from MSBs bits (x+y) and 2. carry from middle
s3 <= v2[WIDTH2] + v3;
end

assign LSBs_Carry = q1[WIDTH1]; // Provide test signals
assign MSBs_Carry = v2[WIDTH2];

// Build a single output word of WIDTH=WIDTH1+WIDTH2+WIDTH3
assign sum ={s3, s2, s1}; // Connect sum to output pins

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: add3p.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// 37-bit adder with three pipeline stages
// uses no components

//`include "220model.v"

module add3p
#(parameter WIDTH      = 37, // Total bit width
          WIDTH0     = 9, // Bit width of LSBs
          WIDTH1     = 9, // Bit width of 2. LSBs
          WIDTH01    = 18, // Sum WIDTH0+WIDTH1
          WIDTH2     = 9, // Bit width of 2. MSBs
          WIDTH012   = 27, // Sum WIDTH0+WIDTH1+WIDTH2

```

```

        WIDTH3    = 10) // Bit width of MSBs
(input  [WIDTH-1:0] x, y, // Inputs
output [WIDTH-1:0] sum, // Result
output LSBs_Carry, Middle_Carry, MSBs_Carry, // Test pins
input      clk); // Clock

reg [WIDTH0-1:0] l0, l1, r0, v0, s0;      // LSBs of inputs
reg [WIDTH0:0] q0;                      // LSBs of inputs
reg [WIDTH1-1:0] l2, l3, r1, s1;        // 2. LSBs of input
reg [WIDTH1:0] v1, q1;                  // 2. LSBs of input
reg [WIDTH2-1:0] l4, l5, s2, h7;        // 2. MSBs bits
reg [WIDTH2:0] q2, v2, r2;              // 2. MSBs bits
reg [WIDTH3-1:0] l6, l7, q3, v3, r3, s3, h8;
                                         // MSBs of input

always @(posedge clk) begin
// Split in MSBs and LSBs and store in registers
// Split LSBs from input x,y
10[WIDTH0-1:0] <= x[WIDTH0-1:0];
11[WIDTH0-1:0] <= y[WIDTH0-1:0];
// Split 2. LSBs from input x,y
12[WIDTH1-1:0] <= x[WIDTH1-1+WIDTH0:WIDTH0];
13[WIDTH1-1:0] <= y[WIDTH1-1+WIDTH0:WIDTH0];
// Split 2. MSBs from input x,y
14[WIDTH2-1:0] <= x[WIDTH2-1+WIDTH01:WIDTH01];
15[WIDTH2-1:0] <= y[WIDTH2-1+WIDTH01:WIDTH01];
// Split MSBs from input x,y
16[WIDTH3-1:0] <= x[WIDTH3-1+WIDTH012:WIDTH012];
17[WIDTH3-1:0] <= y[WIDTH3-1+WIDTH012:WIDTH012];

//***** First stage of the adder *****
q0 <= {1'b0, 10} + {1'b0, 11}; // Add LSBs of x and y
q1 <= {1'b0, 12} + {1'b0, 13}; // Add 2. LSBs of x / y
q2 <= {1'b0, 14} + {1'b0, 15}; // Add 2. MSBs of x/y
q3 <= 16 + 17;                // Add MSBs of x and y
//***** Second stage of the adder *****
v0 <= q0[WIDTH0-1:0];           // Save q0
// Add result from 2. LSBs (x+y) and carry from LSBs
v1 <= q0[WIDTH0] + {1'b0, q1[WIDTH1-1:0]};
// Add result from 2. MSBs (x+y) and carry from 2. LSBs
v2 <= q1[WIDTH1] + {1'b0, q2[WIDTH2-1:0]};
// Add result from MSBs (x+y) and carry from 2. MSBs
v3 <= q2[WIDTH2] + q3;

```

```

//***** Third stage of the adder *****
r0 <= v0; // Delay for LSBs
r1 <= v1[WIDTH1-1:0]; // Delay for 2. LSBs
// Add result from 2. MSBs (x+y) and carry from 2. LSBs
r2 <= v1[WIDTH1] + {1'b0, v2[WIDTH2-1:0]};
// Add result from MSBs (x+y) and carry from 2. MSBs
r3 <= v2[WIDTH2] + v3;
//***** Fourth stage of the adder *****
s0 <= r0; // Delay for LSBs
s1 <= r1; // Delay for 2. LSBs
s2 <= r2[WIDTH2-1:0]; // Delay for 2. MSBs
// Add result from MSBs (x+y) and carry from 2. MSBs
s3 <= r2[WIDTH2] + r3;
end

assign LSBs_Carry = q0[WIDTH1]; // Provide test signals
assign Middle_Carry = v1[WIDTH1];
assign MSBs_Carry = r2[WIDTH2];

// Build a single output word of
// WIDTH = WIDTH0 + WIDTH1 + WIDTH2 + WIDTH3
assign sum = {s3, s2, s1, s0}; // Connect sum to output

endmodule

```

```

//*****
// IEEE STD 1364-2001 Verilog file: mul_ser.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module mul_ser //----> Interface
  (input      clk, reset,
   input  signed [7:0]  x,
   input  [7:0]  a,
   output reg signed [15:0] y);

  always @ (posedge clk) //-> Multiplier in behavioral style
  begin : States
    parameter s0=0, s1=1, s2=2;
    reg [2:0] count;
    reg [1:0] s; // FSM state register
    reg signed [15:0] p, t; // Double bit width
    reg [7:0] a_reg;

    if (reset) // Asynchronous reset

```

```

    s <= s0;
  else
    case (s)
      s0 : begin          // Initialization step
        a_reg <= a;
        s <= s1;
        count = 0;
        p <= 0;           // Product register reset
        t <= x;           // Set temporary shift register to x
      end
      s1 : begin          // Processing step
        if (count == 7)   // Multiplication ready
          s <= s2;
        else
          begin
            if (a_reg[0] == 1) // Use LSB for bit select
              p <= p + t;    // Add 2^k
            a_reg <= a_reg >>> 1;
            t <= t <<< 1;
            count = count + 1;
            s <= s1;
          end
        end
      s2 : begin          // Output of result to y and
        y <= p;           // start next multiplication
        s <= s0;
      end
    endcase
  end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: div_res.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// Restoring Division
// Bit width: WN          WD          WN          WD
//             Numerator / Denominator = Quotient and Remainder
// OR:       Numerator = Quotient * Denominator + Remainder

module div_res(
  input      clk, reset,
  input [7:0] n_in,
  input [5:0] d_in,

```

```
output reg [5:0] r_out,
output reg [7:0] q_out);

parameter s0=0, s1=1, s2=2, s3=3; // State assignments

// Divider in behavioral style
always @(posedge clk or posedge reset)
begin : F // Finite state machine
    reg [3:0] count;
    reg [1:0] s;           // FSM state
    reg [13:0] d;          // Double bit width unsigned
    reg signed [13:0] r; // Double bit width signed
    reg [7:0] q;

    if (reset)           // Asynchronous reset
        s <= s0;
    else
        case (s)
            s0 : begin      // Initialization step
                s <= s1;
                count = 0;
                q <= 0;        // Reset quotient register
                d <= d_in << 7; // Load aligned denominator
                r <= n_in;      // Remainder = numerator
            end
            s1 : begin      // Processing step
                r <= r - d;    // Subtract denominator
                s <= s2;
            end
            s2 : begin      // Restoring step
                if (r < 0) begin // Check r < 0
                    r <= r + d; // Restore previous remainder
                    q <= q << 1; // LSB = 0 and SLL
                end
                else
                    q <= (q << 1) + 1; // LSB = 1 and SLL
                count = count + 1;
                d <= d >> 1;

                if (count == 8) // Division ready ?
                    s <= s3;
                else
                    s <= s1;
            end
        endcase
    end
end
```

```

    s3 : begin      // Output of result
        q_out <= q[7:0];
        r_out <= r[5:0];
        s <= s0;    // Start next division
    end
endcase
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: div_aegp.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// Convergence division after
//           Anderson, Earle, Goldschmidt, and Powers
// Bit width:   WN          WD          WN          WD
//           Numerator / Denominator = Quotient and Remainder
// OR:         Numerator = Quotient * Denominator + Remainder

module div_aegp
(input      clk, reset,
 input [8:0] n_in,
 input [8:0] d_in,
 output reg [8:0] q_out);

always @ (posedge clk or posedge reset) // -> Divider in
begin : States                      // behavioral style
    parameter s0=0, s1=1, s2=2;
    reg [1:0] count;
    reg [1:0] state;
    reg [9:0] x, t, f;           // one guard bit
    reg [17:0] tempx, tempt;

    if (reset)                  // Asynchronous reset
        state <= s0;
    else
        case (state)
            s0 : begin           // Initialization step
                state <= s1;
                count = 0;
                t <= {1'b0, d_in}; // Load denominator
                x <= {1'b0, n_in}; // Load numerator
            end
            s1 : begin           // Processing step

```

```

        f = 512 - t;           // TWO - t
        tempx = (x * f);    // Product in full
        tempt = (t * f);    // bitwidth
        x <= tempx >> 8;   // Fractional f
        t <= tempt >> 8;   // Scale by 256
        count = count + 1;
        if (count == 2)      // Division ready ?
            state <= s2;
        else
            state <= s1;
    end
    s2 : begin           // Output of result
        q_out <= x[8:0];
        state <= s0;     // Start next division
    end
endcase
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: cordic.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module cordic #(parameter W = 7) // Bit width - 1
(input      clk,
 input  signed [W:0] x_in, y_in,
 output reg signed [W:0] r, phi, eps);

// There is bit access in Quartus array types
// in Verilog 2001, therefore use single vectors
// but use a separate line for each array!
reg signed [W:0] x [0:3];
reg signed [W:0] y [0:3];
reg signed [W:0] z [0:3];

always @(posedge clk) begin //----> Infer registers
    if (x_in >= 0)          // Test for x_in < 0 rotate
        begin                // 0, +90, or -90 degrees
            x[0] <= x_in; // Input in register 0
            y[0] <= y_in;
            z[0] <= 0;
        end
    else if (y_in >= 0)

```

```

begin
x[0] <= y_in;
y[0] <= - x_in;
z[0] <= 90;
end
else
begin
x[0] <= - y_in;
y[0] <= x_in;
z[0] <= -90;
end

if (y[0] >= 0) // Rotate 45 degrees
begin
x[1] <= x[0] + y[0];
y[1] <= y[0] - x[0];
z[1] <= z[0] + 45;
end
else
begin
x[1] <= x[0] - y[0];
y[1] <= y[0] + x[0];
z[1] <= z[0] - 45;
end

if (y[1] >= 0) // Rotate 26 degrees
begin
x[2] <= x[1] + (y[1] >>> 1); // i.e. x[1] + y[1] /2
y[2] <= y[1] - (x[1] >>> 1); // i.e. y[1] - x[1] /2
z[2] <= z[1] + 26;
end
else
begin
x[2] <= x[1] - (y[1] >>> 1); // i.e. x[1] - y[1] /2
y[2] <= y[1] + (x[1] >>> 1); // i.e. y[1] + x[1] /2
z[2] <= z[1] - 26;
end

if (y[2] >= 0) // Rotate 14 degrees
begin
x[3] <= x[2] + (y[2] >>> 2); // i.e. x[2] + y[2]/4
y[3] <= y[2] - (x[2] >>> 2); // i.e. y[2] - x[2]/4
z[3] <= z[2] + 14;
end

```

```

    else
      begin
        x[3] <= x[2] - (y[2] >>> 2); // i.e. x[2] - y[2]/4
        y[3] <= y[2] + (x[2] >>> 2); // i.e. y[2] + x[2]/4
        z[3] <= z[2] - 14;
      end

      r    <= x[3];
      phi <= z[3];
      eps <= y[3];
    end

  endmodule

//*****
// IEEE STD 1364-2001 Verilog file: arctan.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module arctan #(parameter W = 9,      // Bit width
                  L = 5)       // Array size
  (input clk,
   input signed [W-1:0] x_in,
   //output reg signed [W-1:0] d_o [1:L],
   output wire signed [W-1:0] d_o1, d_o2 ,d_o3, d_o4 ,d_o5,
   output reg signed [W-1:0] f_out);

  reg signed [W-1:0] x;    // Auxilary signals
  wire signed [W-1:0] f;
  wire signed [W-1:0] d [1:L]; // Auxilary array
  // Chebychev coefficients c1, c2, c3 for 8-bit precision
  // c1 = 212; c3 = -12; c5 = 1;

  always @(posedge clk) begin
    x <= x_in;      // FF for input and output
    f_out <= f;
  end

  // Compute sum-of-products with
  // Clenshaw's recurrence formula
  assign d[5] = 'sd1; // c5=1
  assign d[4] = (x * d[5]) / 128;
  assign d[3] = ((x * d[4]) / 128) - d[5] - 12; // c3=-12
  assign d[2] = ((x * d[3]) / 128) - d[4];
  assign d[1] = ((x * d[2]) / 128) - d[3] + 212; // c1=212
  assign f    = ((x * d[1]) / 256) - d[2];

```

```

// last step is different

assign d_o1 = d[1]; // Provide test signals as outputs
assign d_o2 = d[2];
assign d_o3 = d[3];
assign d_o4 = d[4];
assign d_o5 = d[5];
endmodule

//*****
// IEEE STD 1364-2001 Verilog file: ln.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module ln #(parameter N = 5, // -- Number of coefficients-1
            parameter W= 17) // -- Bitwidth -1
    (input clk,
     input signed [W:0] x_in,
     output reg signed [W:0] f_out);

    reg signed [W:0] x, f; // Auxilary register
    wire signed [W:0] p [0:5];
    reg signed [W:0] s [0:5];

    // Polynomial coefficients for 16-bit precision:
    // f(x) = (1 + 65481 x -32093 x^2 + 18601 x^3
    //           -8517 x^4 + 1954 x^5)/65536
    assign p[0] = 18'sd1;
    assign p[1] = 18'sd65481;
    assign p[2] = -18'sd32093;
    assign p[3] = 18'sd18601;
    assign p[4] = -18'sd8517;
    assign p[5] = 18'sd1954;

    always @(posedge clk)
    begin : Store
        x <= x_in; // Store input in register
    end

    always @(posedge clk)      // Compute sum-of-products
    begin : SOP
        integer k; // define the loop variable
        reg signed [35:0] slv;
        slv[N] = p[N];

```

```

// Polynomial Approximation from Chebyshev coefficients
for (k=N-1; k>=0; k=k-1)
begin
    slv    = x * s[k+1]; // no FFs for slv
    s[k]   = (slv >>> 16) + p[k];
end      // x*s/65536 problem 32 bits
f_out   <= s[0];        // make visable outside
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: sqrt.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****


module sqrt  ////> Interface
(input      clk, reset,
 input [16:0] x_in,
 output [16:0] a_o, imm_o, f_o,
 output reg [2:0] ind_o,
 output reg [1:0] count_o,
 output [16:0] x_o, pre_o, post_o,
 output reg [16:0] f_out);

// Define the operation modes:
parameter load=0, mac=1, scale=2, denorm=3, nop=4;
// Assign the FSM states:
parameter start=0, leftshift=1, sop=2,
          rightshift=3, done=4;

reg [2:0] s, op;
reg [16:0] x; // Auxilary
reg signed [16:0] a, b, f, imm; // ALU data
reg [16:0] pre, post;
// Chebychev poly coefficients for 16-bit precision:
wire signed [16:0] p [0:4];

assign p[0] = 7563;
assign p[1] = 42299;
assign p[2] = -29129;
assign p[3] = 15813;
assign p[4] = -3778;

always @ (posedge reset or posedge clk) //-----> SQRT FSM

```

```

begin : States                                // sample at clk rate
  reg signed [3:0] ind;
  reg [1:0] count;

  if (reset)                               // Asynchronous reset
    s <= start;
  else begin
    case (s)                         // Next State assignments
      start : begin           // Initialization step
        s <= leftshift; ind = 4;
        imm <= x_in;          // Load argument in ALU
        op <= load; count = 0;
      end
      leftshift : begin      // Normalize to 0.5 .. 1.0
        count = count + 1; a <= pre; op <= scale;
        imm <= p[4];
        if (count == 3) begin // Normalize ready ?
          s <= sop; op <= load; x <= f;
        end
      end
      sop : begin            // Processing step
        ind = ind - 1; a <= x;
        if (ind == -1) begin // SOP ready ?
          s <= rightshift; op <= denorm; a <= post;
        end else begin
          imm <= p[ind]; op <= mac;
        end
      end
      rightshift : begin // Denormalize to original range
        s <= done; op <= nop;
      end
      done : begin           // Output of results
        f_out <= f;          // I/O store in register
        op<=nop;
        s <= start;
      end                      // start next cycle
    endcase
  end
  ind_o <= ind;
  count_o <= count;
end

always @(posedge clk) // Define the ALU operations
begin : ALU

```

```

case (op)
    load   : f  <= imm;
    mac    : f  <= (a * f / 32768) + imm;
    scale  : f  <= a * f;
    denorm : f  <= (a * f /32768);
    nop    : f  <= f;
    default: f  <= f;
endcase
end

always @*
begin : EXP
    reg [16:0] slv;
    reg [16:0] po, pr;
    integer K, L;

    slv = x_in;
    // Compute pre-scaling:
    for (K=0; K <= 15; K= K+1)
        if (slv[K] == 1)
            L <= K;
    pre = 1 << (14-L);
    // Compute post scaling:
    po = 1;
    for (K=0; K <= 7; K= K+1) begin
        if (slv[2*K] == 1)      // even 2^k gets 2^k/2
            po = 1 << (K+8);
    //  sqrt(2): CSD Error = 0.0000208 = 15.55 effective bits
    // +1 +0. -1 +0 -1 +0 +1 +0 +1 +0 +0 +0 +0 +1
    //  9      7      5      3      1          -5
        if (slv[2*K+1] == 1) // odd k has sqrt(2) factor
            po = (1<<(K+9)) - (1<<(K+7)) - (1<<(K+5))
                + (1<<(K+3)) + (1<<(K+1)) + (1<<(K-5));
    end
    post <= po;
end

assign a_o = a;    // Provide some test signals as outputs
assign imm_o = imm;
assign f_o = f;
assign pre_o = pre;
assign post_o = post;
assign x_o = x;

```

```

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: fir_gen.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// This is a generic FIR filter generator
// It uses W1 bit data/coefficients bits
module fir_gen
#(parameter W1 = 9,    // Input bit width
      W2 = 18,   // Multiplier bit width 2*W1
      W3 = 19,   // Adder width = W2+log2(L)-1
      W4 = 11,   // Output bit width
      L = 4,     // Filter length
      Mpipeline = 3) // Pipeline steps of multiplier
(input clk, Load_x, // std_logic
 input signed [W1-1:0] x_in, c_in, // Inputs
 output signed [W4-1:0] y_out); // Results

reg signed [W1-1:0] x;
wire signed [W3-1:0] y;
// 1D array types i.e. memories supported by Quartus
// in Verilog 2001; first bit then vector size
reg signed [W1-1:0] c [0:3]; // Coefficient array
wire signed [W2-1:0] p [0:3]; // Product array
reg signed [W3-1:0] a [0:3]; // Adder array

wire signed [W2-1:0] sum; // Auxilary signals
wire clken, aclr;

assign sum=0; assign aclr=0; // Default for mult
assign clken=0;

//----> Load Data or Coefficient
always @(posedge clk)
begin: Load
  if (! Load_x) begin
    c[3] <= c_in; // Store coefficient in register
    c[2] <= c[3]; // Coefficients shift one
    c[1] <= c[2];
    c[0] <= c[1];
  end
  else begin
    x <= x_in; // Get one data sample at a time
  end
end

```

```

    end

//----> Compute sum-of-products
always @(posedge clk)
begin: SOP
// Compute the transposed filter additions
  a[0] <= p[0] + a[1];
  a[1] <= p[1] + a[2];
  a[2] <= p[2] + a[3];
  a[3] <= p[3]; // First TAP has only a register
end
assign y = a[0];

genvar I; //Define loop variable for generate statement
generate
  for (I=0; I<L; I=I+1) begin: MulGen
// Instantiate L pipelined multiplier
  lpm_mult mul_I           // Multiply x*c[I] = p[I]
    (.clock(clk), .dataaa(x), .datab(c[I]), .result(p[I]));
// .sum(sum), .clken(clken), .aclr(aclr)); // Unused ports
  defparam mul_I.lpm_widtha = W1;
  defparam mul_I.lpm_widthb = W1;
  defparam mul_I.lpm_widthp = W2;
  defparam mul_I.lpm_widths = W2;
  defparam mul_I.lpm_pipeline = Mpipeline;
  defparam mul_I.lpm_representation = "SIGNED";
end
endgenerate

assign y_out = y[W3-1:W3-W4];

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: fir_srg.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module fir_srg           //----> Interface
  (input      clk,
   input signed [7:0] x,
   output reg signed [7:0] y);

// Tapped delay line array of bytes
  reg signed [7:0] tap [0:3];
// For bit access use single vectors in Verilog

```

```

integer I;

always @(posedge clk) //----> Behavioral style
begin : p1
  // Compute output y with the filter coefficients weight.
  // The coefficients are [-1 3.75 3.75 -1].
  // Multiplication and division for Altera MaxPlusII can
  // be done in Verilog 2001 with signed shifts !
  y <= (tap[1] <<< 1) + tap[1] + (tap[1] >>> 1) - tap[0]
    + ( tap[1] >>> 2) + (tap[2] <<< 1) + tap[2]
    + (tap[2] >>> 1) + (tap[2] >>> 2) - tap[3];

  for (I=3; I>0; I=I-1) begin
    tap[I] <= tap[I-1]; // Tapped delay line: shift one
  end
  tap[0] <= x; // Input in register 0
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: dafsm.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
`include "case3.v" // User-defined component

module dafsm //--> Interface
  (input      clk, reset,
   input [2:0] x_in0, x_in1, x_in2,
   output [2:0] lut,
   output reg [5:0] y);

  reg [2:0] x0, x1, x2;
  wire [2:0] table_in, table_out;

  reg [5:0] p; // temporary register

  assign table_in[0] = x0[0];
  assign table_in[1] = x1[0];
  assign table_in[2] = x2[0];

  always @(posedge clk or posedge reset)
  begin : DA //----> DA in behavioral style
    parameter s0=0, s1=1;
    reg [0:0] state;

```

```

    reg [1:0] count; // Counts the shifts

    if (reset) // Asynchronous reset
        state <= s0;
    else
        case (state)
            s0 : begin // Initialization
                state <= s1;
                count = 0;
                p <= 0;
                x0 <= x_in0;
                x1 <= x_in1;
                x2 <= x_in2;
            end
            s1 : begin // Processing step
                if (count == 3) begin // Is sum of product done?
                    y <= p; // Output of result to y and
                    state <= s0; // start next sum of product
                end
                else begin
                    p <= (p >> 1) + (table_out << 2); // p/2+table*4
                    x0[0] <= x0[1];
                    x0[1] <= x0[2];
                    x1[0] <= x1[1];
                    x1[1] <= x1[2];
                    x2[0] <= x2[1];
                    x2[1] <= x2[2];
                    count = count + 1;
                    state <= s1;
                end
            end
        endcase
    end

    case3 LC_Table0
    ( .table_in(table_in), .table_out(table_out));

    assign lut = table_out; // Provide test signal

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: case3.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****

```

```

module case3
  (input  [2:0] table_in, // Three bit
   output reg [2:0] table_out); // Range 0 to 6

// This is the DA CASE table for
// the 3 coefficients: 2, 3, 1

  always @(table_in)
  begin
    case (table_in)
      0 :     table_out =  0;
      1 :     table_out =  2;
      2 :     table_out =  3;
      3 :     table_out =  5;
      4 :     table_out =  1;
      5 :     table_out =  3;
      6 :     table_out =  4;
      7 :     table_out =  6;
    default : ;
  endcase
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: case5p.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module case5p
  (input          clk,
   input  [4:0] table_in,
   output reg [4:0] table_out); // range 0 to 25

  reg [3:0] lsbs;
  reg [1:0] msbs0;
  reg [4:0] table0out00, table0out01;

// These are the distributed arithmetic CASE tables for
// the 5 coefficients: 1, 3, 5, 7, 9

  always @ (posedge clk) begin
    lsbs[0] = table_in[0];
    lsbs[1] = table_in[1];
    lsbs[2] = table_in[2];
    lsbs[3] = table_in[3];
  end

```

```
    msbs0[0] = table_in[4];
    msbs0[1] = msbs0[0];
end

// This is the final DA MPX stage.
always @(posedge clk) begin
    case (msbs0[1])
        0 : table_out <= table0out00;
        1 : table_out <= table0out01;
        default : ;
    endcase
end

// This is the DA CASE table 00 out of 1.
always @(posedge clk) begin
    case (lsbs)
        0 : table0out00 = 0;
        1 : table0out00 = 1;
        2 : table0out00 = 3;
        3 : table0out00 = 4;
        4 : table0out00 = 5;
        5 : table0out00 = 6;
        6 : table0out00 = 8;
        7 : table0out00 = 9;
        8 : table0out00 = 7;
        9 : table0out00 = 8;
        10 : table0out00 = 10;
        11 : table0out00 = 11;
        12 : table0out00 = 12;
        13 : table0out00 = 13;
        14 : table0out00 = 15;
        15 : table0out00 = 16;
        default ;
    endcase
end

// This is the DA CASE table 01 out of 1.
always @(posedge clk) begin
    case (lsbs)
        0 : table0out01 = 9;
        1 : table0out01 = 10;
        2 : table0out01 = 12;
        3 : table0out01 = 13;
        4 : table0out01 = 14;
```

```

5  : table0out01 = 15;
6  : table0out01 = 17;
7  : table0out01 = 18;
8  : table0out01 = 16;
9  : table0out01 = 17;
10 : table0out01 = 19;
11 : table0out01 = 20;
12 : table0out01 = 21;
13 : table0out01 = 22;
14 : table0out01 = 24;
15 : table0out01 = 25;
default ;
endcase
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: darom.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
//`include "220model.v"

module darom  //--> Interface
  (input      clk, reset,
   input [2:0] x_in0, x_in1, x_in2,
   output [2:0] lut,
   output reg [5:0] y);

  reg [2:0] x0, x1, x2;
  wire [2:0] table_in, table_out;

  reg [5:0] p; // Temporary register
  wire ena;

  assign ena=1;

  assign table_in[0] = x0[0];
  assign table_in[1] = x1[0];
  assign table_in[2] = x2[0];

  always @(posedge clk or posedge reset)
  begin : DA          //----> DA in behavioral style
    parameter s0=0, s1=1;
    reg [0:0] state;

```

```

    reg [1:0] count; // Counts the shifts

    if (reset)           // Asynchronous reset
        state <= s0;
    else
        case (state)
            s0 : begin // Initialization
                state <= s1;
                count = 0;
                p   <= 0;
                x0 <= x_in0;
                x1 <= x_in1;
                x2 <= x_in2;
            end
            s1 : begin           // Processing step
                if (count == 3) begin // Is sum of product done?
                    y <= (p >> 1) + (table_out << 2); // Output to y
                    state <= s0; // and start next sum of product
                end
                else begin
                    p <= (p >> 1) + (table_out << 2);
                    x0[0] <= x0[1];
                    x0[1] <= x0[2];
                    x1[0] <= x1[1];
                    x1[1] <= x1[2];
                    x2[0] <= x2[1];
                    x2[1] <= x2[2];
                    count = count + 1;
                    state <= s1;
                end
            end
            default : ;
        endcase
    end

    lpm_rom rom_1 // Used ports:
    ( .outclock(clk), .address(table_in), .q(table_out));
// .inclock(clk), .memenab(ena)); // Unused
    defparam rom_1.lpm_width = 3;
    defparam rom_1.lpm_widthad = 3;
    defparam rom_1.lpm_outdata = "REGISTERED";
    defparam rom_1.lpm_address_control = "UNREGISTERED";
    defparam rom_1.lpm_file = "darom3.mif";

```

```
assign lut = table_out; // Provide test signal

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: dasign.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
`include "case3s.v" // User-defined component

module dasign          // -> Interface
  (input      clk, reset,
   input signed [3:0] x_in0, x_in1, x_in2,
   output [3:0] lut,
   output reg signed [6:0] y);

  reg signed [3:0] x0, x1, x2;
  wire signed [2:0] table_in;
  wire signed [3:0] table_out;

  reg [6:0] p; // Temporary register

  assign table_in[0] = x0[0];
  assign table_in[1] = x1[0];
  assign table_in[2] = x2[0];

  always @ (posedge clk or posedge reset) // DA in behavioral
  begin : DA                         // style
    parameter s0=0, s1=1;
    integer k;
    reg [0:0] state;
    reg [2:0] count;                  // Counts the shifts

    if (reset)                      // Asynchronous reset
      state <= s0;
    else
      case (state)
        s0 : begin                  // Initialization step
          state <= s1;
          count = 0;
          p  <= 0;
          x0 <= x_in0;
          x1 <= x_in1;
          x2 <= x_in2;
        end
  end
```

```

    s1 : begin           // Processing step
        if (count == 4) begin// Is sum of product done?
            y <= p;          // Output of result to y and
            state <= s0;      // start next sum of product
        end else begin //Subtract for last accumulator step
            if (count ==3)   // i.e. p/2 +/- table_out * 8
                p <= (p >>> 1) - (table_out <<< 3);
            else           // Accumulation for all other steps
                p <= (p >>> 1) + (table_out <<< 3);
            for (k=0; k<=2; k= k+1) begin      // Shift bits
                x0[k] <= x0[k+1];
                x1[k] <= x1[k+1];
                x2[k] <= x2[k+1];
            end
            count = count + 1;
            state <= s1;
        end
    end
    endcase
end

case3s LC_Table0
( .table_in(table_in), .table_out(table_out));

assign lut = table_out; // Provide test signal

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: case3s.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module case3s
(input [2:0] table_in, // Three bit
 output reg [3:0] table_out); // Range -2 to 4 -> 4 bits

// This is the DA CASE table for
// the 3 coefficients: -2, 3, 1

always @(table_in)
begin
    case (table_in)
        0 :     table_out =  0;
        1 :     table_out = -2;
        2 :     table_out =  3;
    endcase
end

```

```

3 :      table_out =  1;
4 :      table_out =  1;
5 :      table_out = -1;
6 :      table_out =  4;
7 :      table_out =  2;
default : ;
endcase
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: dapara.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
`include "case3s.v" // User-defined component

module dapara           //----> Interface
  (input      clk,
   input signed [3:0] x_in,
   output reg signed[6:0] y);

  reg signed [2:0] x [0:3];
  wire signed [3:0] h [0:3];
  reg signed [4:0] s0, s1;
  reg signed [3:0] t0, t1, t2, t3;

  always @ (posedge clk) //----> DA in behavioral style
  begin : DA
    integer k,l;
    for (l=0; l<=3; l=l+1) begin      // For all 4 vectors
      for (k=0; k<=1; k=k+1) begin    // shift all bits
        x[l][k] <= x[l][k+1];
      end
    end
    for (k=0; k<=3; k=k+1) begin    // Load x_in in the
      x[k][2] <= x_in[k];          // MSBs of the registers
    end
  // y <= h[0] + (h[1] <<< 1) + (h[2] <<< 2) - (h[3] <<< 3);
  // Sign extensions, pipeline register, and adder tree:
    t0 <= h[0]; t1 <= h[1]; t2 <= h[2]; t3 <= h[3];
    s0 <= t0 + (t1 <<< 1);
    s1 <= t2 - (t3 <<< 1);
    y <= s0 + (s1 <<< 2);
  end

```

```

genvar i;// Need to declare loop variable in Verilog 2001
generate      // One table for each bit in x_in
    for (i=0; i<=3; i=i+1) begin:LC_Tables
        case3s LC_Table0 (.table_in(x[i]), .table_out(h[i]));
    end
endgenerate

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: iir.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module iir #(parameter W = 14)      // Bit width - 1
    ( input  signed [W:0] x_in, // Input
      output signed [W:0] y_out, // Result
      input       clk);

    reg signed [W:0] x, y;

    // initial begin
    // y=0;
    // x=0;
    // end

    // Use FFs for input and recursive part
    always @ (posedge clk) begin      // Note: there is a signed
        x  <= x_in;                // integer in Verilog 2001
        y  <= x + (y >>> 1) + (y >>> 2); // >>> uses fewer LEs
    //y  <= x + y / 2 + y / 4; // div with / uses more LEs
    end

    assign y_out = y;           // Connect y to output pins

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: iir_pipe.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module iir_pipe      //----> Interface

```

```

#(parameter W = 14) // Bit width - 1
(input          clk,
 input signed [W:0] x_in,      // Input
 output signed [W:0] y_out); // Result

reg signed [W:0] x, x3, sx;
reg signed [W:0] y, y9;

always @(posedge clk) // Infer FFs for input, output and
begin                // pipeline stages;
  x    <= x_in;           // use nonblocking FF assignments
  x3   <= (x >>> 1) + (x >>> 2);           // i.e. x / 2 + x / 4 = x*3/4
  sx   <= x + x3; // Sum of x element i.e. output FIR part
  y9   <= (y >>> 1) + (y >>> 4);           // i.e. y / 2 + y / 16 = y*9/16
  y    <= sx + y9;           // Compute output
end

assign y_out = y ; // Connect register y to output pins

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: iir_par.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module iir_par      //----> Interface
#(parameter W = 14) // bit width - 1
(input          clk, reset,
 input signed [W:0] x_in,
 output signed [W:0] y_out,
 output         clk2);

reg signed [W:0] x_even, xd_even, x_odd, xd_odd, x_wait;
reg signed [W:0] y_even, y_odd, y_wait, y;
reg signed [W:0] sum_x_even, sum_x_odd;
reg             clk_div2;

always @(posedge clk)           // Clock divider by 2
begin : clk_divider            // for input clk
  clk_div2 <= ! clk_div2;
end

always @(posedge clk)           // Split x into even

```

```

begin : Multiplex           // and odd samples;
parameter even=0, odd=1;    // recombine y at clk rate
reg [0:0] state;

if (reset)                  // Asynchronous reset
    state <= even;
else
    case (state)
        even : begin
            x_even <= x_in;
            x_odd <= x_wait;
            y <= y_wait;
            state <= odd;
        end
        odd : begin
            x_wait <= x_in;
            y <= y_odd;
            y_wait <= y_even;
            state <= even;
        end
    endcase
end

assign y_out = y;
assign clk2 = clk_div2;

always @ (negedge clk_div2)
begin: Arithmetic
    xd_even <= x_even;
    sum_x_even <= x_odd + (xd_even >>> 1) + (xd_even >>> 2);
                // i.e. x_odd + x_even / 2 + x_even / 4
    y_even <= sum_x_even + (y_even >>> 1) + (y_even >>> 4);
                // i.e. sum_x_even + y_even / 2 + y_even / 16
    xd_odd <= x_odd;
    sum_x_odd <= xd_even + (xd_odd >>> 1) + (xd_odd >>> 4);
                // i.e. x_even + xd_odd / 2 + xd_odd / 4
    y_odd <= sum_x_odd + (y_odd >>> 1) + (y_odd >>> 4);
                // i.e. sum_x_odd + y_odd / 2 + y_odd / 16
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: cic3r32.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org

```

```

//*****
module cic3r32 //----> Interface
  (input      clk, reset,
   input signed [7:0] x_in,
   output signed [9:0] y_out,
   output reg clk2);

  parameter hold=0, sample=1;
  reg [1:0] state;
  reg [4:0] count;
  reg signed [7:0] x;      // Registered input
  reg signed [25:0] i0, i1 , i2; // I section 0, 1, and 2
  reg signed [25:0] i2d1, i2d2, c1, c0;      // I + COMB 0
  reg signed [25:0] c1d1, c1d2, c2;      // COMB section 1
  reg signed [25:0] c2d1, c2d2, c3;      // COMB section 2

  always @(posedge clk or posedge reset)
begin : FSM
  if (reset) begin           // Asynchronous reset
    count <= 0;
    state <= hold;
    clk2 <= 0;
  end else begin
    if (count == 31) begin
      count <= 0;
      state <= sample;
      clk2 <= 1;
    end else begin
      count <= count + 1;
      state <= hold;
      clk2 <= 0;
    end
  end
end

always @(posedge clk) // 3 integrator sections
begin : Int
  x     <= x_in;
  i0    <= i0 + x;
  i1    <= i1 + i0 ;
  i2    <= i2 + i1 ;
end

always @(posedge clk) // 3 comb sections

```

```

begin : Comb
  if (state == sample) begin
    c0    <= i2;
    i2d1 <= c0;
    i2d2 <= i2d1;
    c1    <= c0 - i2d2;
    c1d1 <= c1;
    c1d2 <= c1d1;
    c2    <= c1 - c1d2;
    c2d1 <= c2;
    c2d2 <= c2d1;
    c3    <= c2 - c2d2;
  end
end

assign y_out = c3[25:16];

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: cic3s32.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module cic3s32           //----> Interface
  (input      clk, reset,
   output reg clk2,
   input  signed [7:0] x_in,
   output signed [9:0] y_out);

parameter hold=0, sample=1;
reg [1:0] state;
reg [4:0] count;
reg signed [7:0] x;                      // Registered input
reg signed [25:0] i0;                     // I section 0
reg signed [20:0] i1;                     // I section 1
reg signed [15:0] i2;                     // I section 2
reg signed [13:0] i2d1, i2d2, c1, c0;    // I+C0
reg signed [12:0] c1d1, c1d2, c2;        // COMB 1
reg signed [11:0] c2d1, c2d2, c3;        // COMB 2

always @(posedge clk or posedge reset)
begin : FSM
  if (reset) begin           // Asynchronous reset
    count <= 0;
    state <= hold;
  end
end

```

```

    clk2  <= 0;
end else begin
  if (count == 31) begin
    count <= 0;
    state <= sample;
    clk2  <= 1;
  end
  else begin
    count <= count + 1;
    state <= hold;
    clk2  <= 0;
  end
end
end

always @(posedge clk) // 3 integrator sections
begin : Int
  x  <= x_in;
  i0 <= i0 + x;
  i1 <= i1 + i0[25:5];
  i2 <= i2 + i1[20:5];
end

always @(posedge clk) // 3 comb sections
begin : Comb
  if (state == sample) begin
    c0  <= i2[15:2];
    i2d1 <= c0;
    i2d2 <= i2d1;
    c1  <= c0 - i2d2;
    c1d1 <= c1[13:1];
    c1d2 <= c1d1;
    c2  <= c1[13:1] - c1d2;
    c2d1 <= c2[12:1];
    c2d2 <= c2d1;
    c3  <= c2[12:1] - c2d2;
  end
end

assign y_out = c3[11:2];

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: db4poly.v

```

```

// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module db4poly      //----> Interface
  (input          clk, reset,
   output         clk2,
   input signed [7:0]  x_in,
   output signed [16:0] x_e, x_o, g0, g1, // Test signals
   output signed [8:0]  y_out);

  reg signed [7:0] x_odd, x_even, x_wait;
  reg   clk_div2;

// Register for multiplier, coefficients, and taps
  reg signed [16:0] m0, m1, m2, m3, r0, r1, r2, r3;
  reg signed [16:0] x33, x99, x107;
  reg signed [16:0] y;

  always @ (posedge clk or posedge reset) // Split into even
  begin : Multiplex           // and odd samples at clk rate
    parameter even=0, odd=1;
    reg [0:0] state;

    if (reset)                  // Asynchronous reset
      state <= even;
    else
      case (state)
        even : begin
          x_even <= x_in;
          x_odd  <= x_wait;
          clk_div2 = 1;
          state <= odd;
        end
        odd : begin
          x_wait <= x_in;
          clk_div2 = 0;
          state <= even;
        end
      endcase
    end

    always @ (x_odd, x_even)
    begin : RAG
// Compute auxiliary multiplications of the filter
      x33  = (x_odd <<< 5) + x_odd;
    end
  end

```

```

x99  = (x33 <<< 1) + x33;
x107 = x99 + (x_odd << 3);
// Compute all coefficients for the transposed filter
m0 = (x_even <<< 7) - (x_even <<< 2); // m0 = 124
m1 = x107 <<< 1;                      // m1 = 214
m2 = (x_even <<< 6) - (x_even <<< 3)
               + x_even; // m2 = 57
m3 = x33;                                // m3 = -33
end

always @ (negedge clk_div2) // Infer registers;
begin : AddPolyphase      // use nonblocking assignments
//----- Compute filter G0
r0 <= r2 + m0;           // g0 = 128
r2 <= m2;                // g2 = 57
//----- Compute filter G1
r1 <= -r3 + m1;          // g1 = 214
r3 <= m3;                // g3 = -33
// Add the polyphase components
y <= r0 + r1;
end

// Provide some test signals as outputs
assign x_e = x_even;
assign x_o = x_odd;
assign clk2 = clk_div2;
assign g0 = r0;
assign g1 = r1;

assign y_out = y >>> 8; // Connect y / 256 to output

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: rc_sinc.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module rc_sinc #(parameter OL = 2, //Output buffer length-1
                  IL = 3, //Input buffer length -1
                  L = 10) // Filter length -1
  (input clk, reset, // Clock + reset for the registers
   input signed [7:0] x_in,
   output [3:0] count_o,
   output ena_in_o, ena_out_o, ena_io_o,
   output signed [8:0] f0_o, f1_o, f2_o,

```

```

    output signed [8:0] y_out);

reg [3:0] count; // Cycle R_1*R_2
reg ena_in, ena_out, ena_io; // FSM enables
reg signed [7:0] x [0:10]; // TAP registers for 3 filters
reg signed [7:0] ibuf [0:3]; // TAP in registers
reg signed [7:0] obuf [0:2]; // TAP out registers
reg signed [8:0] f0, f1, f2; // Filter outputs

// Constant arrays for multiplier and taps:
wire signed [8:0] c0 [0:10];
wire signed [8:0] c2 [0:10];

// filter coefficients for filter c0
assign c0[0] = -19; assign c0[1] = 26; assign c0[2]=-42;
assign c0[3] = 106; assign c0[4] = 212; assign c0[5]=-53;
assign c0[6] = 29; assign c0[7] = -21; assign c0[8]=16;
assign c0[9] = -13; assign c0[10] = 11;

// filter coefficients for filter c2
assign c2[0] = 11; assign c2[1] = -13;assign c2[2] = 16;
assign c2[3] = -21;assign c2[4] = 29; assign c2[5] = -53;
assign c2[6] = 212;assign c2[7] = 106;assign c2[8] = -42;
assign c2[9] = 26; assign c2[10] = -19;

always @ (posedge reset or posedge clk)
begin : FSM // Control the system and sample at clk rate
  if (reset)           // Asynchronous reset
    count <= 0;
  else begin
    if (count == 11)
      count <= 0;
    else
      count <= count + 1;
  end
end

always @ (posedge clk)
begin      // set the enable signal for the TAP lines
  case (count)
    2, 5, 8, 11 : ena_in <= 1;
    default      : ena_in <= 0;
  endcase

```

```

    case (count)
        4, 8      : ena_out <= 1;
        default   : ena_out <= 0;
    endcase

    if (count == 0)
        ena_io <= 1;
    else
        ena_io <= 0;
    end

always @ (posedge clk)           //----> Input delay line
begin : INPUTMUX
    integer I;      // loop variable

    if (ena_in) begin
        for (I=IL; I>=1; I=I-1)
            ibuf[I] <= ibuf[I-1];          // shift one
        ibuf[0] <= x_in;                // Input in register 0
    end
end

always @ (posedge clk)           //----> Output delay line
begin : OUPUTMUX
    integer I;      // loop variable

    if (ena_io) begin // store 3 samples in output buffer
        obuf[0] <= f0;
        obuf[1] <= f1;
        obuf[2] <= f2;
    end
    else if (ena_out) begin
        for (I=OL; I>=1; I=I-1)
            obuf[I] <= obuf[I-1];          // shift one
    end
end

always @ (posedge clk)           //----> One tapped delay line
begin : TAP                    // get 4 samples at one time
    integer I;      // loop variable

    if (ena_io) begin
        for (I=0; I<=3; I=I+1)
            x[I] <= ibuf[I];          // take over input buffer
    end
end

```

```

    for (I=4; I<=10; I=I+1) // 0->4; 4->8 etc.
        x[I] <= x[I-4];           // shift 4 taps

    end
end

always @(posedge clk) // Compute sum-of-products for f0
begin : SOP0
    reg signed [16:0] sum; // temp sum
    reg signed [16:0] p [0:10]; // temp products
    integer I;

    for (I=0; I<=L; I=I+1) // Infer L+1 multiplier
        p[I] = c0[I] * x[I];

    sum = p[0];
    for (I=1; I<=L; I=I+1)      // Compute the direct
        sum = sum + p[I];          // filter adds

    f0 <= sum >>> 8;
end

always @(posedge clk) // Compute sum-of-products for f1
begin : SOP1
    f1 <= x[5]; // No scaling, i.e., unit impulse
end

always @(posedge clk) // Compute sum-of-products for f2
begin : SOP2
    reg signed[16:0] sum; // temp sum
    reg signed [16:0] p [0:10]; // temp products
    integer I;

    for (I=0; I<=L; I=I+1) // Infer L+1 multiplier
        p[I] = c2[I] * x[I];

    sum = p[0];
    for (I=1; I<=L; I=I+1)      // Compute the direct
        sum = sum + p[I];          // filter adds

    f2 <= sum >>> 8;
end

```

```

// Provide some test signals as outputs
assign f0_o = f0;
assign f1_o = f1;
assign f2_o = f2;
assign count_o = count;
assign ena_in_o = ena_in;
assign ena_out_o = ena_out;
assign ena_io_o = ena_io;

assign y_out = obuf[OL]; // Connect to output

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: farrow.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module farrow #(parameter IL = 3) // Input buffer length -1
    (input clk, reset, // Clock/reset for the registers
     input signed [7:0] x_in,
     output [3:0] count_o,
     output ena_in_o, ena_out_o,
     output signed [8:0] c0_o, c1_o, c2_o, c3_o,
     output [8:0] d_out,
     output reg signed [8:0] y_out);

    reg [3:0] count; // Cycle R_1*R_2
    wire [6:0] delta; // Increment d
    reg ena_in, ena_out; // FSM enables
    reg signed [7:0] x [0:3];
    reg signed [7:0] ibuf [0:3]; // TAP registers
    reg [8:0] d; // Fractional Delay scaled to 8 bits
    // Lagrange matrix outputs:
    reg signed [8:0] c0, c1, c2, c3;

    assign delta = 85;

    always @ (posedge reset or posedge clk)      // Control the
    begin : FSM                                // system and sample at clk rate
        reg [8:0] dnew;
        if (reset) begin                         // Asynchronous reset
            count <= 0;
            d <= delta;
        end else begin
            if (count == 11)

```

```

        count <= 0;
    else
        count <= count + 1;
    if (ena_out) begin      // Compute phase delay
        dnew = d + delta;
        if (dnew >= 255)
            d <= 0;
        else
            d <= dnew;
    end
end
end

always @ (posedge clk)
begin           // Set the enable signals for the TAP lines
    case (count)
        2, 5, 8, 11 : ena_in <= 1;
        default      : ena_in <= 0;
    endcase

    case (count)
        3, 7, 11 : ena_out <= 1;
        default   : ena_out <= 0;
    endcase
end

always @ (posedge clk)      //-----> One tapped delay line
begin : TAP
    integer I;      // loop variable

    if (ena_in) begin
        for (I=1; I<=IL; I=I+1)
            ibuf[I-1] <= ibuf[I];    // Shift one

        ibuf[IL] <= x_in;          // Input in register IL
    end
end

always @ (posedge clk)
begin : GET           // Get 4 samples at one time
    integer I;      // loop variable

    if (ena_out) begin

```

```

for (I=0; I<=IL; I=I+1)
    x[I] <= ibuf[I]; // take over input buffer
end
end

// Compute sum-of-products:
always @(posedge clk) // Compute sum-of-products for f0
begin : SOP
    reg signed [8:0] y; // temp's

// Matrix multiplier iV=inv(Vandermonde) c=iV*x(n-1:n+2)'
//      x(0)      x(1)      x(2)      x(3)
// iV=      0       1.0000      0       0
//      -0.3333   -0.5000   1.0000   -0.1667
//      0.5000   -1.0000   0.5000      0
//     -0.1667    0.5000   -0.5000   0.1667
    if (ena_out) begin

        c0 <= x[1];
        c1 <= (-85 * x[0] >>> 8) - (x[1]/2) + x[2] -
                                         (43 * x[3] >>> 8);
        c2 <= ((x[0] + x[2]) >>> 1) - x[1];
        c3 <= ((x[1] - x[2]) >>> 1) +
                                         (43 * (x[3] - x[0]) >>> 8);

// Farrow structure = Lagrange with Horner schema
// for u=0:3, y=y+f(u)*d^u; end;
        y = c2 + ((c3 * d) >>> 8); // d is scale by 256
        y = ((y * d) >>> 8) + c1;
        y = ((y * d) >>> 8) + c0;

        y_out <= y; // Connect to output + store in register
    end
end

assign c0_o = c0; // Provide test signals as outputs
assign c1_o = c1;
assign c2_o = c2;
assign c3_o = c3;
assign count_o = count;
assign ena_in_o = ena_in;
assign ena_out_o = ena_out;
assign d_out = d;

```

```

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: cmoms.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module cmoms #(parameter IL = 3) // Input buffer length -1
    (input clk, reset, // Clock/reset for registers
     input signed [7:0] x_in,
     output [3:0] count_o,
     output ena_in_o, ena_out_o,
     output signed [8:0] c0_o, c1_o, c2_o, c3_o, xiir_o,
     output signed [8:0] y_out);

    reg [3:0] count; // Cycle R_1*R_2
    reg [1:0] t;
    reg ena_in, ena_out; // FSM enables
    reg signed [7:0] x [0:3];
    reg signed [7:0] ibuf [0:3]; // TAP registers
    reg signed [8:0] xiir; // iir filter output

    reg signed [16:0] y, y0, y1, y2, y3, h0, h1; // temp's

    // Spline matrix output:
    reg signed [8:0] c0, c1, c2, c3;

    // Precomputed value for d**k :
    wire signed [8:0] d1 [0:2];
    wire signed [8:0] d2 [0:2];
    wire signed [8:0] d3 [0:2];

    assign d1[0] = 0; assign d1[1] = 85; assign d1[2] = 171;
    assign d2[0] = 0; assign d2[1] = 28; assign d2[2] = 114;
    assign d3[0] = 0; assign d3[1] = 9; assign d3[2] = 76;

    always @(posedge reset or posedge clk) // Control the
    begin : FSM                                // system sample at clk rate
        if (reset) begin                      // Asynchronous reset
            count <= 0;
            t <= 1;
        end else begin
            if (count == 11)
                count <= 0;
        end
    end

```

```

    else
        count <= count + 1;
    if (ena_out)
        if (t>=2)      // Compute phase delay
            t <= 0;
        else
            t <= t + 1;
    end
end
assign t_out = t;

always @(posedge clk) // set the enable signal
begin                  // for the TAP lines
    case (count)
        2, 5, 8, 11 : ena_in <= 1;
        default       : ena_in <= 0;
    endcase

    case (count)
        3, 7, 11     : ena_out <= 1;
        default       : ena_out <= 0;
    endcase
end

// Coeffs: H(z)=1.5/(1+0.5z^-1)
always @(posedge clk)      //----> Behavioral Style
begin : IIR // Compute iir coefficients first
reg signed [8:0] x1;      // x * 1

if (ena_in) begin
    xiir <= (3 * x1 >>> 1) - (xiir >>> 1);
    x1 = x_in;
end
end

always @(posedge clk)      //----> One tapped delay line
begin : TAP
integer I;    // loop variable

if (ena_in) begin
    for (I=1; I<=IL; I=I+1)
        ibuf[I-1] <= ibuf[I]; // Shift one

    ibuf[IL] <= xiir;        // Input in register IL

```

```

    end
end

always @ (posedge clk)      //----> One tapped delay line
begin : GET                // get 4 samples at one time
    integer I;      // loop variable

    if (ena_out) begin
        for (I=0; I<=IL; I=I+1)
            x[I] <= ibuf[I]; // take over input buffer
        end
    end

// Compute sum-of-products:
always @ (posedge clk) // Compute sum-of-products for f0
begin : SOP
// Matrix multiplier C-MOMS matrix:
//   x(0)      x(1)      x(2)      x(3)
//   0.3333    0.6667    0          0
//   -0.8333   0.6667   0.1667    0
//   0.6667   -1.5      1.0       -0.1667
//   -0.1667   0.5      -0.5      0.1667
    if (ena_out) begin

        c0 <= (85 * x[0] + 171 * x[1]) >>> 8;
        c1 <= (171 * x[1] - 213 * x[0] + 43 * x[2]) >>> 8;
        c2 <= (171 * x[0] - (43 * x[3]) >>> 8)
                - (3 * x[1] >>> 1) + x[2];
        c3 <= (43 * (x[3] - x[0])) >>> 8)
                + ((x[1] - x[2]) >>> 1);

// No Farrow structure, parallel LUT for delays
// for u=0:3, y=y+f(u)*d^u; end;

        y0 <= c0 * 256; // Use pipelined adder tree
        y1 <= c1 * d1[t];
        y2 <= c2 * d2[t];
        y3 <= c3 * d3[t];
        h0 <= y0 + y1;
        h1 <= y2 + y3;
        y <= h0 + h1;
    end
end
assign y_out = y >>> 8; // Connect to output

```

```

assign c0_o = c0; // Provide some test signals as outputs
assign c1_o = c1;
assign c2_o = c2;
assign c3_o = c3;
assign count_o = count;
assign ena_in_o = ena_in;
assign ena_out_o = ena_out;
assign xiir_o = xiir;

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: db4latti.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module db4latti
  (input          clk, reset,
   output         clk2,
   input signed [7:0] x_in,
   output signed [16:0] x_e, x_o,
   output reg signed [8:0] g, h);

  reg signed [7:0] x_wait;
  reg signed [16:0] sx_up, sx_low;
  reg clk_div2;
  wire signed [16:0] sxa0_up, sxa0_low;
  wire signed [16:0] up0, up1, low1;
  reg signed [16:0] low0;

  always @(posedge clk or posedge reset) // Split into even
  begin : Multiplex           // and odd samples at clk rate
    parameter even=0, odd=1;
    reg [0:0] state;

    if (reset)                  // Asynchronous reset
      state <= even;
    else
      case (state)
        even : begin
          // Multiply with 256*s=124
          sx_up  <= (x_in <<< 7) - (x_in <<< 2);
          sx_low <= (x_wait <<< 7) - (x_wait <<< 2);
          clk_div2 <= 1;
          state <= odd;
        end
      endcase
    end
  end
endmodule

```

```

        end
    odd : begin
        x_wait <= x_in;
        clk_div2 <= 0;
        state <= even;
    end
endcase
end

//***** Multiply a[0] = 1.7321
// Compute: (2*sx_up - sx_up /4)-(sx_up /64 + sx_up /256)
assign sxa0_up = ((sx_up <<< 1) - (sx_up >>> 2))
            - ((sx_up >>> 6) + (sx_up >>> 8));
// Compute: (2*sx_low - sx_low/4)-(sx_low/64 + sx_low/256)
assign sxa0_low = ((sx_low <<< 1) - (sx_low >>> 2))
            - ((sx_low >>> 6) + (sx_low >>> 8));

//***** First stage -- FF in lower tree
assign up0 = sxa0_low + sx_up;
always @(negedge clk_div2)
begin: LowerTreeFF
    low0 <= sx_low - sxa0_up;
end

//***** Second stage: a[1]=-0.2679
// Compute: (up0 - low0/4) - (low0/64 + low0/256);
assign up1 = (up0 - (low0 >>> 2))
            - ((low0 >>> 6) + (low0 >>> 8));
// Compute: (low0 + up0/4) + (up0/64 + up0/256)
assign low1 = (low0 + (up0 >>> 2))
            + ((up0 >>> 6) + (up0 >>> 8));

assign x_e = sx_up;           // Provide some extra
assign x_o = sx_low;          // test signals
assign clk2 = clk_div2;

always @(negedge clk_div2)
begin: OutputScale
    g <= up1 >>> 8;        // i.e. up1 / 256
    h <= low1 >>> 8;       // i.e. low1 / 256;
end

endmodule
//*****

```

```

// IEEE STD 1364-2001 Verilog file: rader7.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module rader7          //---> Interface
  (input      clk, reset,
   input [7:0] x_in,
   output reg signed [10:0] y_real, y_imag);

  reg signed [10:0] accu;           // Signal for X[0]
  // Direct bit access of 2D vector in Quartus Verilog 2001
  // possible no auxiliary signal for this purpose necessary
  reg signed [18:0] im [0:5];
  reg signed [18:0] re [0:5];
  // real is keyword in Verilog and can not be an identifier
  // Tapped delay line array
  reg signed [18:0] x57, x111, x160, x200, x231, x250 ;
                           // The filter coefficients
  reg signed [18:0] x5, x25, x110, x125, x256;
                           // Auxiliary filter coefficients
  reg signed [7:0]  x, x_0;        // Signals for x[0]

  always @(posedge clk or posedge reset) // State machine
  begin : States                      // for RADER filter
    parameter Start=0, Load=1, Run=2;
    reg [1:0] state;
    reg [4:0] count;

    if (reset)                         // Asynchronous reset
      state <= Start;
    else
      case (state)
        Start : begin               // Initialization step
          state <= Load;
          count <= 1;
          x_0 <= x_in;             // Save x[0]
          accu <= 0;                // Reset accumulator for X[0]
          y_real  <= 0;
          y_imag  <= 0;
        end
        Load : begin // Apply x[5],x[4],x[6],x[2],x[3],x[1]
          if (count == 8)           // Load phase done ?
            state <= Run;
          else begin
            state <= Load;
          end
        end
      endcase
  end
endmodule

```

```

        accu <= accu + x;
    end
    count <= count + 1;
end
Run : begin // Apply again x[5],x[4],x[6],x[2],x[3]
    if (count == 15) begin // Run phase done ?
        y_real <= accu;           // X[0]
        y_imag <= 0;             // Only re inputs => Im(X[0])=0
        state <= Start;         // Output of result
    end                               // and start again
    else begin
        y_real <= (re[0] >>> 8) + x_0;
                                         // i.e. re[0]/256+x[0]
        y_imag <= (im[0] >>> 8);      // i.e. im[0]/256
        state <= Run;
    end
    count <= count + 1;
end
endcase
end

always @ (posedge clk)      // Structure of the two FIR
begin : Structure          // filters in transposed form
    x <= x_in;
    // Real part of FIR filter in transposed form
    re[0] <= re[1] + x160 ;   // W^1
    re[1] <= re[2] - x231 ;   // W^3
    re[2] <= re[3] - x57 ;    // W^2
    re[3] <= re[4] + x160 ;   // W^6
    re[4] <= re[5] - x231 ;   // W^4
    re[5] <= -x57;           // W^5

    // Imaginary part of FIR filter in transposed form
    im[0] <= im[1] - x200 ;   // W^1
    im[1] <= im[2] - x111 ;   // W^3
    im[2] <= im[3] - x250 ;   // W^2
    im[3] <= im[4] + x200 ;   // W^6
    im[4] <= im[5] + x111 ;   // W^4
    im[5] <= x250;            // W^5
end

always @ (posedge clk)      // Note that all signals
begin : Coeffs              // are globally defined
// Compute the filter coefficients and use FFs

```

```

x160  <= x5 <<< 5;           // i.e. 160 = 5 * 32;
x200  <= x25 <<< 3;           // i.e. 200 = 25 * 8;
x250  <= x125 <<< 1;          // i.e. 250 = 125 * 2;
x57   <= x25 + (x <<< 5); // i.e. 57 = 25 + 32;
x111  <= x110 + x;            // i.e. 111 = 110 + 1;
x231  <= x256 - x25;          // i.e. 231 = 256 - 25;
end

always @*                         // Note that all signals
begin : Factors                  // are globally defined
// Compute the auxiliary factor for RAG without an FF
  x5  = (x <<< 2) + x; // i.e. 5 = 4 + 1;
  x25 = (x5 <<< 2) + x5; // i.e. 25 = 5*4 + 5;
  x110 = (x25 <<< 2) + (x5 <<< 2); // i.e. 110 = 25*4+5*4;
  x125 = (x25 <<< 2) + x25; // i.e. 125 = 25*4+25;
  x256 = x <<< 8;           // i.e. 256 = 2 ** 8;
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: ccmul.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
//`include "220model.v"

module ccmul #(parameter W2 = 17,    // Multiplier bit width
                 W1 = 9,      // Bit width c+s sum
                 W = 8)      // Input bit width
  (input clk, // Clock for the output register
   input signed [W-1:0] x_in, y_in, c_in, // Inputs
   input signed [W1-1:0] cps_in, cms_in, // Inputs
   output reg signed [W-1:0] r_out, i_out); // Results

  wire signed [W-1:0] x, y, c ;           // Inputs and outputs
  wire signed [W2-1:0] r, i, cmsy, cpsx, xmvc, sum; //Prod.
  wire signed [W1-1:0] xmvc, cps, cms, sctx, sctxy; //x-y etc.

  wire clken, cr1, ovl1, cin1, aclr, ADD, SUB;
                                // Auxiliary signals
  assign cin1=0; assign aclr=0; assign ADD=1; assign SUB=0;
  assign cr1=0; assign sum=0; assign clken=0;
                                // Default for add

```

```

assign x    = x_in;    // x
assign y    = y_in;    // j * y
assign c    = c_in;    // cos
assign cps = cps_in; // cos + sin
assign cms = cms_in; // cos - sin

always @(posedge clk) begin
    r_out <= r[W2-3:W-1];           // Scaling and FF for output
    i_out <= i[W2-3:W-1];
end

//***** ccmul with 3 mul. and 3 add/sub *****
assign sxtx = x;      // Possible growth for
assign sxtv = y;      // sub_1 -> sign extension

lpm_add_sub sub_1          // Sub: x - y
( .result(xmy), .dataaa(sxtx), .dataab(sxtv)); // Used ports
// .add_sub(SUB), .cout(cr1), .overflow(ovl1), .cin(cin1),
// .clken(clken), .clock(clk), .aclr(aclr)); // Unused
defparam sub_1.lpm_width = W1;
defparam sub_1.lpm_representation = "SIGNED";
defparam sub_1.lpm_direction = "sub";

lpm_mult mul_1           // Multiply (x-y)*c = xmyc
( .dataaa(xmy), .dataab(c), .result(xmyc)); // Used ports
// .sum(sum), .clock(clk), .clken(clken), .aclr(aclr));
//                                         // Unused ports
defparam mul_1.lpm_widtha = W1;
defparam mul_1.lpm_widthb = W;
defparam mul_1.lpm_widthhp = W2;
defparam mul_1.lpm_widthhs = W2;
defparam mul_1.lpm_representation = "SIGNED";

lpm_mult mul_2           // Multiply (c-s)*y = cmsy
( .dataaa(cms), .dataab(y), .result(cmsy)); // Used ports
// .sum(sum), .clock(clk), .clken(clken), .aclr(aclr));
//                                         // Unused ports
defparam mul_2.lpm_widtha = W1;
defparam mul_2.lpm_widthb = W;
defparam mul_2.lpm_widthhp = W2;
defparam mul_2.lpm_widthhs = W2;
defparam mul_2.lpm_representation = "SIGNED";

lpm_mult mul_3           // Multiply (c+s)*x = cpsx

```

```

( .dataaa(cps), .datab(x), .result(cpsx)); // Used ports
// .sum(sum), .clock(clk), .clken(clken), .aclr(aclr));
//                                         // Unused ports

defparam mul_3.lpm_widtha= W1;
defparam mul_3.lpm_widthb = W;
defparam mul_3.lpm_widthp = W2;
defparam mul_3.lpm_widths = W2;
defparam mul_3.lpm_representation = "SIGNED";

lpm_add_sub add_1           // Add: r <= (x-y)*c + (c-s)*y
( .dataaa(cmsy), .datab(xmyc), .result(r)); // Used ports
// .add_sub(ADD), .cout(cr1), .overflow(ovl1), .cin(cin1),
// .clken(clken), .clock(clk), .aclr(aclr)); // Unused
defparam add_1.lpm_width = W2;
defparam add_1.lpm_representation = "SIGNED";
defparam add_1.lpm_direction = "add";

lpm_add_sub sub_2           // Sub: i <= (c+s)*x - (x-y)*c
( .dataaa(cpsx), .datab(xmyc), .result(i)); // Used ports
// .add_sub(SUB), .cout(cr1), .overflow(ovl1), .clock(clk),
// .cin(cin1), .clken(clken), .aclr(aclr)); // Unused
defparam sub_2.lpm_width = W2;
defparam sub_2.lpm_representation = "SIGNED";
defparam sub_2.lpm_direction = "sub";

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: bfproc.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
//`include "220model.v"
//`include "ccmul.v"

module bfproc #(parameter W2 = 17, // Multiplier bit width
                  W1 = 9,    // Bit width c+s sum
                  W = 8)    // Input bit width
  (input clk, // Clock for the output register
   input signed [W-1:0] Are_in, Aim_in,      // 8-bit inputs
   input signed [W-1:0] Bre_in, Bim_in, c_in, // 8-bit inputs
   input signed [W1-1:0] cps_in, cms_in, // coefficients
   output reg signed [W-1:0] Dre_out, Dim_out, // registered
   output signed [W-1:0] Ere_out, Eim_out); // results

  reg signed [W-1:0] dif_re, dif_im;        // Bf out

```

```

reg signed [W-1:0] Are, Aim, Bre, Bim; // Inputs integer
reg signed [W-1:0] c; // Input
reg signed [W1-1:0] cps, cms; // Coefficient in

always @(posedge clk) // Compute the additions of the
begin // butterfly using integers
    Are <= Are_in; // and store inputs
    Aim <= Aim_in; // in flip-flops
    Bre <= Bre_in;
    Bim <= Bim_in;
    c <= c_in; // Load from memory cos
    cps <= cps_in; // Load from memory cos+sin
    cms <= cms_in; // Load from memory cos-sin
    Dre_out <= (Are >>> 1) + (Bre >>> 1); // Are/2 + Bre/2
    Dim_out <= (Aim >>> 1) + (Bim >>> 1); // Aim/2 + Bim/2
end

// No FF because butterfly difference "diff" is not an
always @(*) // output port
begin
    dif_re = (Are >>> 1) - (Bre >>> 1); // i.e. Are/2 - Bre/2
    dif_im = (Aim >>> 1) - (Bim >>> 1); // i.e. Aim/2 - Bim/2
end

//*** Instantiate the complex twiddle factor multiplier
ccmul ccmul_1 // Multiply (x+jy)(c+js)
(.clk(clk), .x_in(dif_re), .y_in(dif_im), .c_in(c),
.cps_in(cps), .cms_in(cms), .r_out(Ere_out),
.i_out(Eim_out));

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: lfsr.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module lfsr //----> Interface
    (input      clk,
     output [6:1] y); // Result

    reg [6:1] ff; // Note that reg is keyword in Verilog and
                    // can not be variable name
    integer i;

    always @(posedge clk) begin // Length-6 LFSR with xor

```

```

ff[1] <= ff[5] ^^ ff[6]; // Use nonblocking assignment
for (i=6; i>=2 ; i=i-1) // Tapped delay line: shift one
    ff[i] <= ff[i-1];
end

assign y = ff;           // Connect to I/O pins

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: lfsr6s3.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module lfsr6s3           //----> Interface
  (input      clk,
   output [6:1] y); // Result

  reg [6:1] ff; // Note that reg is keyword in Verilog and
                 // can not be variable name

  always @(posedge clk) begin // Implement three-step
    ff[6] <= ff[3];          // length-6 LFSR with xnor;
    ff[5] <= ff[2];          // use nonblocking assignments
    ff[4] <= ff[1];
    ff[3] <= ff[5] ^^ ff[6];
    ff[2] <= ff[4] ^^ ff[5];
    ff[1] <= ff[3] ^^ ff[4];
  end

  assign y = ff;

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: ammod.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
module ammod #(parameter W = 8) // Bit width - 1
  (input      clk,           //----> Interface
   input signed [W:0] r_in,
   input signed [W:0] phi_in,
   output reg signed [W:0] x_out, y_out, eps);

  reg signed [W:0] x [0:3]; // There is bit access in 2D

```

```

reg signed [W:0] y [0:3]; // array types in
reg signed [W:0] z [0:3]; // Quartus Verilog 2001

always @(posedge clk) begin //----> Infer register
    if (phi_in > 90)           // Test for |phi_in| > 90
        begin                  // Rotate 90 degrees
            x[0] <= 0;
            y[0] <= r_in;          // Input in register 0
            z[0] <= phi_in - 'sd90;
        end
    else
        if (phi_in < - 90)
            begin
                x[0] <= 0;
                y[0] <= - r_in;
                z[0] <= phi_in + 'sd90;
            end
        else
            begin
                x[0] <= r_in;
                y[0] <= 0;
                z[0] <= phi_in;
            end
    if (z[0] >= 0)           // Rotate 45 degrees
        begin
            x[1] <= x[0] - y[0];
            y[1] <= y[0] + x[0];
            z[1] <= z[0] - 'sd45;
        end
    else
        begin
            x[1] <= x[0] + y[0];
            y[1] <= y[0] - x[0];
            z[1] <= z[0] + 'sd45;
        end
    if (z[1] >= 0)           // Rotate 26 degrees
        begin
            x[2] <= x[1] - (y[1] >>> 1); // i.e. x[1] - y[1] /2
            y[2] <= y[1] + (x[1] >>> 1); // i.e. y[1] + x[1] /2
            z[2] <= z[1] - 'sd26;
        end
    else

```

```

begin
  x[2] <= x[1] + (y[1] >>> 1); // i.e. x[1] + y[1] /2
  y[2] <= y[1] - (x[1] >>> 1); // i.e. y[1] - x[1] /2
  z[2] <= z[1] + 'sd26;
end

if (z[2] >= 0)                                // Rotate 14 degrees
begin
  x[3] <= x[2] - (y[2] >>> 2); // i.e. x[2] - y[2]/4
  y[3] <= y[2] + (x[2] >>> 2); // i.e. y[2] + x[2]/4
  z[3] <= z[2] - 'sd14;
end
else
begin
  x[3] <= x[2] + (y[2] >>> 2); // i.e. x[2] + y[2]/4
  y[3] <= y[2] - (x[2] >>> 2); // i.e. y[2] - x[2]/4
  z[3] <= z[2] + 'sd14;
end

  x_out <= x[3];
  eps    <= z[3];
  y_out <= y[3];
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: fir_lms.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// This is a generic LMS FIR filter generator
// It uses W1 bit data/coefficients bits

module fir_lms      //----> Interface
  #(parameter W1 = 8,   // Input bit width
         W2 = 16,  // Multiplier bit width 2*W1
         L = 2,    // Filter length
         Delay = 3) // Pipeline steps of multiplier
  (input clk, // 1 bit input
   input signed [W1-1:0] x_in, d_in, // Inputs
   output signed [W2-1:0] e_out, y_out, // Results
   output signed [W1-1:0] f0_out, f1_out); // Results

// Signed data types are supported in 2001
// Verilog, and used whenever possible

```

```

reg signed [W1-1:0] x [0:1]; // Data array
reg signed [W1-1:0] f [0:1]; // Coefficient array
reg signed [W1-1:0] d;
wire signed [W1-1:0] emu;
wire signed [W2-1:0] p [0:1]; // 1. Product array
wire signed [W2-1:0] xemu [0:1]; // 2. Product array
wire signed [W2-1:0] y, sxtys, e, sxtde;

wire clken, aclr;
wire signed [W2-1:0] sum; // Auxilary signals

assign sum=0; assign aclr=0; // Default for mult
assign clken=0;

always @(posedge clk) // Store these data or coefficients
begin: Store
    d <= d_in; // Store desired signal in register
    x[0] <= x_in; // Get one data sample at a time
    x[1] <= x[0]; // shift 1
    f[0] <= f[0] + xemu[0][15:8]; // implicit divide by 2
    f[1] <= f[1] + xemu[1][15:8];
end

// Instantiate L pipelined multiplier
genvar I;
generate
    for (I=0; I<L; I=I+1) begin: Mul_fx
        lpm_mult mul_xf // Multiply x[I]*f[I] = p[I]
        (.dataaa(x[I]), .datab(f[I]), .result(p[I]));
        // .clock(clk), .sum(sum),
        // .clken(clken), .aclr(aclr)); // Unused ports
        defparam mul_xf.lpm_widtha = W1;
        defparam mul_xf.lpm_widthb = W1;
        defparam mul_xf.lpm_widthp = W2;
        defparam mul_xf.lpm_widths = W2;
        // defparam mul_xf.lpm_pipeline = Delay;
        defparam mul_xf.lpm_representation = "SIGNED";
    end // for loop
endgenerate

assign y = p[0] + p[1]; // Compute ADF output

```

```

// Scale y by 128 because x is fraction
assign e = d - (y >>> 7) ;
assign emu = e >>> 1; // e*mu divide by 2 and
                        // 2 from xemu makes mu=1/4

// Instantiate L pipelined multiplier
generate
    for (I=0; I<L; I=I+1) begin: Mul_xemu
        lpm_mult mul_I           // Multiply xemu[I] = emu * x[I];
        (.dataaa(x[I]), .dataab(emu), .result(xemu[I]));
//        .clock(clk), .sum(sum),
//        .clken(clken), .aclr(aclr)); // Unused ports
        defparam mul_I.lpm_widtha = W1;
        defparam mul_I.lpm_widthb = W1;
        defparam mul_I.lpm_widthp = W2;
        defparam mul_I.lpm_widths = W2;
//        defparam mul_I.lpm_pipeline = Delay;
        defparam mul_I.lpm_representation = "SIGNED";
        end // for loop
    endgenerate

    assign y_out = y;      // Monitor some test signals
    assign e_out = e;
    assign f0_out = f[0];
    assign f1_out = f[1];

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: fir6dlms.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// This is a generic DLMS FIR filter generator
// It uses W1 bit data/coefficients bits

module fir6dlms      //----> Interface
#(parameter W1 = 8,   // Input bit width
         W2 = 16,  // Multiplier bit width 2*W1
         L = 2,    // Filter length
         Delay = 3) // Pipeline steps of multiplier
(input clk, // 1 bit input
 input signed [W1-1:0] x_in, d_in, // Inputs
 output signed [W2-1:0] e_out, y_out, // Results
 output signed [W1-1:0] f0_out, f1_out); // Results

```

```

// 2D array types memories are supported by Quartus II
// in Verilog, use therefore single vectors
reg signed [W1-1:0] x [0:4], f0, f1;
reg signed [W1-1:0] f[0:1];
reg signed [W1-1:0] d[0:3]; // Desired signal array
wire signed [W1-1:0] emu;
wire signed [W2-1:0] xemu[0:1]; // Product array
wire signed [W2-1:0] p[0:1]; // Product array
wire signed [W2-1:0] y, sxt, e, sxt;
wire clken, aclr;
wire signed [W2-1:0] sum; // Auxilary signals

assign sum=0; assign aclr=0; // Default for mult
assign clken=0;

always @ (posedge clk) // Store these data or coefficients
begin: Store
    d[0] <= d_in; // Shift register for desired data
    d[1] <= d[0];
    d[2] <= d[1];
    d[3] <= d[2];
    x[0] <= x_in; // Shift register for data
    x[1] <= x[0];
    x[2] <= x[1];
    x[3] <= x[2];
    x[4] <= x[3];
    f[0] <= f[0] + xemu[0][15:8]; // implicit divide by 2
    f[1] <= f[1] + xemu[1][15:8];
end

// Instantiate L pipelined multiplier
genvar I;
generate
    for (I=0; I<L; I=I+1) begin: Mul_fx
        lpm_mult mul_xf // Multiply x[I]*f[I] = p[I]
        (.clock(clk), .dataaa(x[I]), .dataab(f[I]), .result(p[I]));
    // .sum(sum), .clken(clken), .aclr(aclr)); // Unused ports
        defparam mul_xf.lpm_widtha = W1;
        defparam mul_xf.lpm_widthb = W1;
        defparam mul_xf.lpm_widthp = W2;
        defparam mul_xf.lpm_widths = W2;
    end
end

```

```

defparam mul_xf.lpm_pipeline = Delay;
defparam mul_xf.lpm_representation = "SIGNED";
end // for loop
endgenerate

assign y = p[0] + p[1]; // Compute ADF output

// Scale y by 128 because x is fraction
assign e = d[3] - (y >>> 7);
assign emu = e >>> 1; // e*mu divide by 2 and
                        // 2 from xemu makes mu=1/4

// Instantiate L pipelined multiplier
generate
    for (I=0; I<L; I=I+1) begin: Mul_xemu
        lpm_mult mul_I           // Multiply xemu[I] = emu * x[I];
        (.clock(clk), .dataaa(x[I+Delay]), .dataab(emu),
         .result(xemu[I]));
    // .sum(sum), .clken(clken), .aclr(aclr)); // Unused ports
        defparam mul_I.lpm_widtha = W1;
        defparam mul_I.lpm_widthb = W1;
        defparam mul_I.lpm_widthp = W2;
        defparam mul_I.lpm_widths = W2;
        defparam mul_I.lpm_pipeline = Delay;
        defparam mul_I.lpm_representation = "SIGNED";
    end // for loop
endgenerate

assign y_out = y; // Monitor some test signals
assign e_out = e;
assign f0_out = f[0];
assign f1_out = f[1];

endmodule

// Description: This is a W x L bit register file.
//***** IEEE STD 1364-2001 Verilog file: reg_file.v *****
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//***** module reg_file #(parameter W = 7, // Bit width -1
N = 15) //Number of register - 1
(input clk, reg_ena,
 input [W:0] data,
 input [3:0] rd, rs, rt ,

```

```

        output reg [W:0] s, t;

reg [W:0] r [0:N];

always @(posedge clk) // Input mux inferring registers
begin : MUX
    if ((reg_ena == 1) & (rd > 0))
        r[rd] <= data;
end

// 2 output demux without registers
always @*
begin : DEMUX
    if (rs > 0) // First source
        s = r[rs];
    else
        s = 0;
    if (rt > 0) // Second source
        t = r[rt];
    else
        t = 0;
end

endmodule

//*****
// IEEE STD 1364-2001 Verilog file: trisc0.v
// Author-EMAIL: Uwe.Meyer-Baese@ieee.org
//*****
// Title: T-RISC stack machine
// Description: This is the top control path/FSM of the
// T-RISC, with a single three-phase clock cycle design
// It has a stack machine/0-address-type instruction word
// The stack has only four words.
//`include "220model.v"

module trisc0 #(parameter WA = 7, // Address bit width -1
                WD = 7)      // Data bit width -1
(input reset, clk, // Clock for the output register
 output jc_OUT, me_ena,
 input [WD:0] iport,
 output reg [WD:0] oport,
 output [WD:0] s0_OUT, s1_OUT, dmd_IN, dmd_OUT,
 output [WA:0] pc_OUT, dma_OUT, dma_IN,
 output [7:0] ir_imm,
```

```

output [3:0] op_code);

//parameter ifetch=0, load=1, store=2, incpc=3;
reg [1:0] state;

wire [3:0] op;
wire [WD:0] imm, dmd;
reg [WD:0] s0, s1, s2, s3;
reg [WA:0] pc;
wire [WA:0] dma;
wire [11:0] pmd, ir;
wire eq, ne, not_clk;
reg mem_ena, jc;

// OP Code of instructions:
parameter
add = 0, neg = 1, sub = 2, opand = 3, opor = 4,
inv = 5, mul = 6, pop = 7, pushi = 8, push = 9,
scan = 10, print = 11, cne = 12, ceq = 13, cjp = 14,
jmp = 15;

// Code of FSM:
always @ (op) // Sequential FSM of processor
    // Check store in register ?
    case (op) // always store except Branch
        pop : mem_ena <= 1;
        default : mem_ena <= 0;
    endcase

always @ (negedge clk or posedge reset)
if (reset == 1) // update the program counter
    pc <= 0;
else begin // use falling edge
    if (((op==cjp) & (jc==0)) | (op==jmp))
        pc <= imm;
    else
        pc <= pc + 1;
end

always @ (posedge clk or posedge reset)
if (reset) // compute jump flag and store in FF
    jc <= 0;
else
    jc <= ((op == ceq) & (s0 == s1)) |

```

```

((op == cne) & (s0 != s1));

// Mapping of the instruction, i.e., decode instruction
assign op = ir[11:8]; // Operation code
assign dma = ir[7:0]; // Data memory address
assign imm = ir[7:0]; // Immidiate operand

lpm_rom prog_rom
( .outclock(clk), .address(pc), .q(pmd)); // Used ports
// .inclock(clk), .memenab(ena)); // Unused
defparam prog_rom.lpm_width = 12;
defparam prog_rom.lpm_widthad = 8;
defparam prog_rom.lpm_outdata = "REGISTERED";
defparam prog_rom.lpm_address_control = "UNREGISTERED";
defparam prog_rom.lpm_file = "TRISCOFAC.MIF";

assign not_clk = ~clk;

lpm_ram_dq data_ram
( .inclock(not_clk), .address(dma), .q(dmd),
  .data(s0), .we(mem_ena)); // Used ports
// .outclock(clk)); // Unused
defparam data_ram.lpm_width = 8;
defparam data_ram.lpm_widthad = 8;
defparam data_ram.lpm_indata = "REGISTERED";
defparam data_ram.lpm_outdata = "UNREGISTERED";
defparam data_ram.lpm_address_control = "REGISTERED";

always @(posedge clk)
begin : P3
    integer temp;

    case (op)
        add      : s0  <= s0 + s1;
        neg      : s0  <= -s0;
        sub      : s0  <= s1 - s0;
        opand   : s0  <= s0 & s1;
        opor    : s0  <= s0 | s1;
        inv     : s0  <= ~ s0;
        mul      : begin temp = s0 * s1; // double width
                    s0  <= temp[WD:0]; end // product
        pop      : s0  <= s1;
        push     : s0  <= dmd;
    endcase
end

```

```
pushi  :  s0  <= imm;
scan   :  s0 <= iport;
print  :  begin oport <= s0; s0<=s1; end
default:  s0 <= 0;
endcase
case (op) // SPECIFY THE STACK OPERATIONS
    pushi, push, scan : begin s3<=s2; s2<=s1; s1<=s0; end
                           // Push type
    cjp, jmp,  inv | neg : ; // Do nothing for branch
    default : begin s1<=s2; s2<=s3; s3<=0; end
                           // Pop all others
endcase
end

// Extra test pins:
assign dmd_OUT = dmd; assign dma_OUT = dma; //Data memory
assign dma_IN = dma; assign dmd_IN = s0;
assign pc_OUT = pc; assign ir = pmd; assign ir_imm = imm;
assign op_code = op; // Program control
// Control signals:
assign jc_OUT = jc; assign me_ena = mem_ena;
// Two top stack elements:
assign s0_OUT = s0; assign s1_OUT = s1;

endmodule
```

## B. VHDL and Verilog Coding

Unfortunately, today we find *two* HDL languages are popular. The US west coast and Asia prefer Verilog, while the US east coast and Europe more frequently use VHDL. For digital signal processing with FPGAs, both languages seem to be well suited, but some VHDL examples were in the past a little easier to read because of the supported signed arithmetic and multiply/divide operations in the IEEE VHDL 1076-1987 and 1076-1993 standards. This gap has disappeared with the introduction of the Verilog IEEE standard 1364-2001, as it also includes signed arithmetic. Other constraints may include personal preferences, EDA library and tool availability, data types, readability, capability, and language extensions using PLIs, as well as commercial, business and marketing issues, to name just a few. A detailed comparison can be found in the book by Smith [3]. Tool providers acknowledge today that both languages need to be supported.

It is therefore a good idea to use an HDL code style that can easily be translated into either language. An important rule is to avoid any keyword in *both* languages in the HDL code when naming variables, labels, constants, user types, etc. The IEEE standard VHDL 1076-1987 uses 77 keywords and an extra 19 keywords are used in VHDL 1076-1993 (see VHDL 1076-1993 Language Reference Manual (LRM) on p. 179). New in VHDL 1076-1993 are:

```
GROUP, IMPURE, INERTIAL, LITERAL, POSTPONED, PURE, REJECT  
ROL, ROR, SHARED, SLA, SLL, SRA, SRL, UNAFFECTED, XNOR,
```

which are unfortunately *not* highlighted in the MaxPlus II editor but with the Quartus II. The IEEE standard Verilog 1364-1995, on the other hand, has 102 keywords (see LRM, p. 604). Together, both HDL languages have 201 keywords, including 19 in common. Table B.1 shows VHDL 1076-1993 keywords in capital letters, Verilog 1364-2001 keywords in small letters, and the common keywords with a capital first letter. New in Verilog 1076-2001 are:

```
automatic, cell, config, design, endconfig, endgenerate,  
generate, genvar, incdir, include, instance, liblist,  
library, localparam, noshowcancelled, pulsetestyle_oneevent,  
pulsetestyle_onedetect, showcancelled, signed, unsigned, use
```

**Table B.1.** VHDL 1076-1993 and Verilog 1364-2001 keywords.

ABS	event	notif0	
ACCESS	EXIT	notif1	SIGNAL
AFTER	FILE	NULL	signed
ALIAS	For	OF	OF
ALL	force	ON	SLA
always	forever	OPEN	SLL
And	fork	Or	small
ARCHITECTURE	Function	OTHERS	specify
ARRAY	Generate	OUT	specparam
ASSERT	GENERIC	output	SRA
assign	genvar	PACKAGE	SRL
ATTRIBUTE	GROUP	parameter	strong0
automatic	GUARDED	pmos	strong1
Begin	highz0	PORT	SUBTYPE
BLOCK	highz1	posedge	supply0
BODY	If	POSTPONED	supply1
buf	ifnone	primitive	table
BUFFER	IMPURE	PROCEDURE	task
bufif0	IN	PROCESS	THEN
bufif1	incdir	pull0	time
BUS	include	pull1	TO
Case	INERTIAL	pulldown	tran
casex	initial	pullup	tranif0
casez	Inout	pulsestyle_onevent	tranif1
cell	input	pulsestyle_onedetect	TRANSPORT
cmos	instance	PURE	tri
config	integer	RANGE	tri0
COMPONENT	IS	rcmos	tri1
CONFIGURATION	join	real	triand
CONSTANT	LABEL	realtime	trior
deassign	large	RECORD	trireg
default	liblist	reg	TYPE
defparam	Library	REGISTER	UNAFFECTED
design	LINKAGE	REJECT	UNITS
disable	LITERAL	release	unsigned
DISCONNECT	LOOP	REM	UNTIL
DOWNTO	localparam	repeat	Use
edge	macromodule	REPORT	VARIABLE
Else	MAP	RETURN	vectored
ELSIF	medium	rnmos	Wait
End	MOD	ROL	wand
endcase	module	ROR	weak0
endconfig	Nand	rpmos	weak1
endfunction	negedge	rtran	WHEN
endgenerate	NEW	rtranif0	While
endmodule	NEXT	rtranif1	wire
endprimitive	nmos	scalared	WITH
endspecify	Nor	SELECT	wor
endtable	noshowcancelled	SEVERITY	Xnor
endtask	Not	SHARED	Xor
ENTITY		showcancelled	

## B.1 List of Examples

These synthesis results for all examples can be easily reproduced by using the scripts `qvhdl.tcl` in the VHDL or Verilog directories of the CD-ROM. Run the TCL script with

```
quartus_sh -t qvhdl.tcl > qvhdl.txt
```

The script produces for each design four parameters. For the `trisc0.vhd`, for instance, we get:

```
....  
-----  
trisc0 fmax: 115.65 MHz ( period = 8.647 ns )  
trisc0 LEs: 198 / 33,216 ( < 1 % )  
trisc0 M4K bits: 5,120 / 483,840 ( 1 % )  
trisc0 DSP blocks: 1 / 70 ( 1 % )  
-----  
....
```

then `grep` through the report `qvhdl.txt` file using `fmax:`, `LEs:` etc.

From the script you will notice that the following special options of Quartus II web edition 6.0 were used:

- Device set Family to Cyclone II and then under Available devices select EP2C35F672C6.
- For Timing Analysis Settings set Default required `fmax:` to 3 ns.
- For Analysis & Synthesis Settings from the Assignments menu
  - set Optimization Technique to Speed
  - Deselect Power-Up Don't Care
- In the Fitter Settings select as Fitter effort Standard Fit (highest effort)

The table below displays the results for all VHDL and Verilog examples given in this book. The table is structured as follows. The first column shows the entity or module name of the design. Columns 2 to 6 are data for the VHDL designs: the number of LEs shown in the report file; the number of 9 × 9-bit multipliers; the number of M4K memory blocks; the Registered Performance; and the page with the source code. The same data are provided for the Verilog design examples, shown in columns 7 to 9. Note that VHDL and Verilog produce the same data for number of 9 × 9-bit multiplier and number of M4K memory blocks, but the LEs and Registered Performance do not always match.

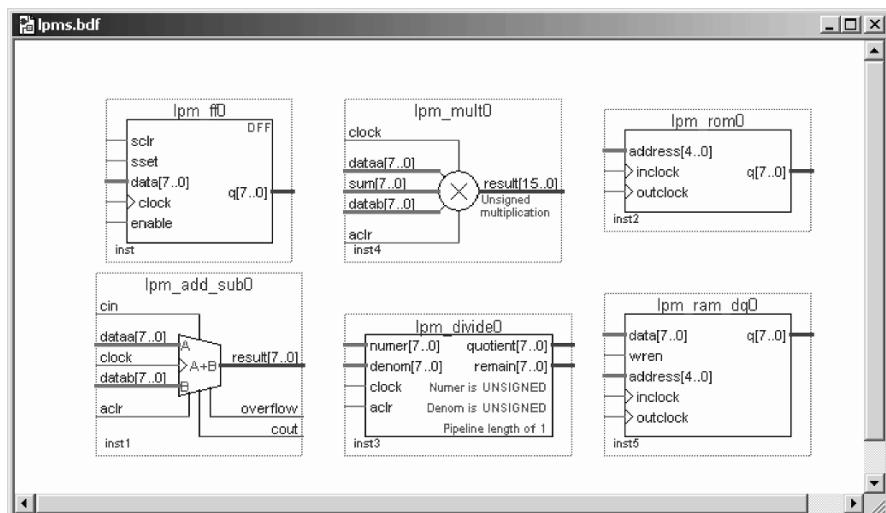
Design	LEs	9 × 9 Mult.	VHDL			Page	Verilog		
			M4Ks	$f_{\text{MAX}}$ MHz	Page		LEs	$f_{\text{MAX}}$ MHz	Page
add_1p	125	no	0	316.46	78	77	390.63	666	
add_2p	234	no	0	229.04	78	144	283.85	667	
add_3p	372	no	0	215.84	78	229	270.42	668	
ammod	316	no	0	215.98	455	277	288.85	717	
arctan	100	4	0	32.09	134	99	32.45	676	
bfproc	131	3	0	95.73	370	83	116.09	715	
ccmul	39	3	0	—	368	39	—	713	
cic3r32	337	no	0	282.17	262	337	269.69	694	
cic3s32	205	no	0	284.58	269	205	284.50	696	
cmoms	372	10	0	85.94	303	239	107.48	705	
cmul7p8	48	no	0	-	59	48	—	665	
cordic	235	no	0	222.67	126	197	317.16	674	
dafsm	32	no	0	420.17	189	30	420.17	683	
dapara	33	no	0	214.96	202	45	420.17	691	
darom	27	no	1	218.29	196	27	218.96	687	
dasign	56	no	0	236.91	199	47	328.19	688	
db4latti	418	no	0	58.81	324	248	74.69	709	
db4poly	173	no	0	136.65	250	158	136.31	697	
div_aegp	64	4	0	134.63	94	64	134.63	671	
div_res	127	no	0	265.32	100	115	257.86	673	
example	24	no	0	420.17	15	24	420.17	663	
farrow	279	6	0	43.91	292	175	65.77	703	
fir6dlms	138	4	0	176.15	511	138	174.52	721	
fir_gen	184	4	0	329.06	167	184	329.06	680	
fir_lms	50	4	0	74.59	504	50	74.03	719	
fir_srg	114	no	0	97.21	179	70	106.15	682	
fun_text	32	no	1	264.20	30	32	264.20	664	
iir	62	no	0	160.69	217	30	234.85	692	
iir_par	268	no	0	168.12	237	199	136.87	693	
iir_pipe	124	no	0	207.08	231	75	354.48	692	
lfsr	6	no	0	420.17	437	6	420.17	716	
lfsr6s3	6	no	0	420.17	440	6	420.17	717	
ln	88	10	0	32.76	145	88	32.76	677	
mul_ser	121	no	0	256.15	82	140	245.34	670	
rader7	443	no	0	137.06	355	404	159.41	710	
rc_sinc	448	19	0	61.93	285	416	81.47	699	
reg_file	211	no	0	-	559	211	—	723	
sqrt	336	2	0	82.16	150	317	82.73	678	
triso	198	1	2	115.65	606	166	71.94	724	

## B.2 Library of Parameterized Modules (LPM)

Throughout the book we use six different LPM megafunctions (see Fig. B.1), namely:

- **lpm\_ff**, the flip-flop megafunction
- **lpm\_add\_sub**, the adder/subtractor megafunction
- **lpm\_ram\_dq**, the RAM megafunction
- **lpm\_rom**, the ROM megafunction
- **lpm\_divide**, the divider megafunction, and
- **lpm\_mult**, the multiplier megafunction

These megafunctions are explained in the following, along with their port definitions, parameters, and resource usage. This information is also available using the Quartus II help under **megafunctions/LPM**.



**Fig. B.1.** Six LPM megafunction used.

### B.2.1 The Parameterized Flip-Flop Megafunction (**lpm\_ff**)

The **lpm\_ff** function is useful if features are needed that are not available in the DFF, DFFE, TFF, and TFFE primitives, such as synchronous or asynchronous set, clear, and load inputs. We have used this megafunction for the following designs: **example**, p. 15 and **fun\_text**, p. 30.

Altera recommends instantiating this function as described in “Using the MegaWizard Plug-In Manager” in the Quartus II help.

The port names and order for Verilog HDL prototypes are:

```
module lpm_ff ( q, data, clock, enable, aclr,
    aset, sclr, sset, aload, sload) ;
```

The VHDL component declaration is shown below:

```
COMPONENT lpm_ff
  GENERIC (LPM_WIDTH: POSITIVE;
           LPM_AVALUE: STRING := "UNUSED";
           LPM_FFTYPE: STRING := "FFTYPE_DFF";
           LPM_TYPE: STRING := "L_FF";
           LPM_SVALUE: STRING := "UNUSED";
           LPM_HINT: STRING := "UNUSED");
  PORT (data: IN STD_LOGIC_VECTOR(LPM_WIDTH-1 DOWNTO 0);
        clock: IN STD_LOGIC;
        enable: IN STD_LOGIC := '1';
        sload: IN STD_LOGIC := '0';
        sclr: IN STD_LOGIC := '0';
        sset: IN STD_LOGIC := '0';
        aload: IN STD_LOGIC := '0';
        aclr: IN STD_LOGIC := '0';
        aset: IN STD_LOGIC := '0';
        q: OUT STD_LOGIC_VECTOR(LPM_WIDTH-1 DOWNTO 0));
  END COMPONENT;
```

## Ports

The following table displays all input ports of `lpm_ff`:

Port name	Required	Description	Comments
<b>data</b>	No	T-type flip-flop: Toggle enable D-type flip-flop: Data input	Input port LPM_WIDTH wide. If the <b>data</b> input is not used, at least one of the <b>aset</b> , <b>aclr</b> , <b>sset</b> , or <b>sclr</b> ports must be used. Unused data inputs default to GND.
<b>clock</b>	Yes	Positive-edge triggered clock	
<b>enable</b>	No	Clock Enable input	Default = 1
<b>sclr</b>	No	Synchronous clear input	If both <b>sset</b> and <b>sclr</b> are used and both are asserted, <b>sclr</b> is dominant. The <b>sclr</b> signal affects the output <b>q</b> values before polarity is applied to the ports.
<b>sset</b>	No	Synchronous set input	Sets <b>q</b> outputs to the value specified by LPM_SVALUE, if that value is present, or sets the <b>q</b> outputs to all 1s. If both <b>sset</b> and <b>sclr</b> are used and both are asserted, <b>sclr</b> is dominant. The <b>sset</b> signal affects the output <b>q</b> values before polarity is applied to the ports.
<b>sload</b>	No	Synchronous load input. Default = 0. If <b>sload</b> is used, <b>data</b> must be used. For load operation, <b>sload</b> must flop with the value be high (1) and enable must be high (1) on the <b>data</b> input or unconnected. The <b>sload</b> port is ignored the next active clock when the LPM_FFTYPE parameter is set to DFF.	
<b>aclr</b>	No	Asynchronous clear input	If both <b>aset</b> and <b>aclr</b> are used and both are asserted, <b>aclr</b> is dominant. The <b>aclr</b> signal affects the output <b>q</b> values before polarity is applied to the ports.
<b>aset</b>	No	Asynchronous set input	Sets <b>q</b> outputs to the value specified by LPM_AVALUE, if that value is present, or sets the <b>q</b> outputs to all 1s.
<b>aload</b>	No	Asynchronous load input. Asynchronously loads the Default = 0. If <b>aload</b> is used, <b>data</b> must be used. For load operation, <b>aload</b> must flop with the value on the <b>data</b> input.	

The following table displays all OUTPUT ports of **lpm\_ff**:

Port Name	Required	Description	Comments
<b>q</b>	Yes	Data output from D or T flip-flops	Output port LPM_WIDTH wide

## Parameters

The following table shows the parameters of the `lpm_ff` component:

Parameter	Type	Required	Description
<code>LPM_WIDTH</code>	Integer	Yes	Width of the <code>data</code> and <code>q</code> ports
<code>LPM_AVALUE</code>	Integer	No	Constant value that is loaded when <code>aset</code> is high. If omitted, defaults to all 1s. The <code>LPM_AVALUE</code> parameter is limited to a maximum of 32 bits.
<code>LPM_SVALUE</code>	Integer	No	Constant value that is loaded on the rising edge of <code>clock</code> when <code>sset</code> is high. If omitted, defaults to all 1s.
<code>LPM_FFTYPE</code>	String	No	Values are DFF, TFF, and UNUSED. Type of flip-flop. If omitted, the default is DFF. When the <code>LPM_FFTYPE</code> parameter is set to DFF, the <code>sload</code> port is ignored.
<code>LPM_HINT</code>	String	No	Allows you to specify Altera-specific parameters in VHDL design files. The default is UNUSED.
<code>LPM_TYPE</code>	String	No	Identifies the LPM entity name in the VHDL design files.

Note that for Verilog LPM 220 synthesizable code (i.e., `220model.v`) the following parameter ordering applies: `lpm_type`, `lpm_width`, `lpm_aval`, `lpm_svalue`, `lpm_pvalue`, `lpm_fftype`, `lpm_hint`.

## Function

The following table is an example of the T-type flip-flop behavior in `lpm_ff`:

Inputs							Outputs
aclr	aset	enable	clock	sclr	sset	sload	<code>Q</code> [ <code>LPM_WIDTH-1..0</code> ]
1	X	X	X	X	X	X	000...
0	1	X	X	X	X	X	111... or <code>LPM_AVALUE</code>
0	0	0	X	X	X	X	<code>q</code> [ <code>LPM_WIDTH-1..0</code> ]
0	0	1	J	1	X	X	000...
0	0	1	J	0	1	X	111... or <code>LPM_SVALUE</code>
0	0	1	J	0	0	1	<code>data</code> [ <code>LPM_WIDTH-1..0</code> ]
0	0	1	J	0	0	0	<code>q</code> [ <code>LPM_WIDTH-1..0</code> ]
							xor <code>data</code> [ <code>LPM_WIDTH-1..0</code> ]

## Resource Usage

The megafunction `lpm_ff` uses one logic cell per bit.

### B.2.2 The Parameterized Adder/Subtractor Megafunction (`lpm_add_sub`)

Altera recommends using the `lpm_add_sub` function to replace all other types of adder/subtractor functions, including old-style adder/subtractor macrofunctions. We have used this megafunction for the following designs: `example`, p. 15, `fun_text`, p. 30, `ccmul`, p. 368.

Altera recommends instantiating this function as described in “Using the MegaWizard Plug-In Manager” in the Quartus II help.

The port names and order for Verilog HDL prototypes are:

```
module lpm_add_sub ( cin,
                     dataaa, datab,
                     add_sub, clock, aclr,
                     result, cout, overflow);
```

The VHDL component declaration is shown below:

```
COMPONENT lpm_add_sub
  GENERIC (LPM_WIDTH: POSITIVE;
           LPM REPRESENTATION: STRING := "SIGNED";
           LPM_DIRECTION: STRING := "UNUSED";
           LPM_HINT: STRING := "UNUSED";
           LPM_PIPELINE: INTEGER := 0;
           LPM_TYPE: STRING := "L_ADD_SUB");
  PORT (dataaa, datab
        : IN STD_LOGIC_VECTOR(LPM_WIDTH-1 DOWNTO 0);
        aclr, clken, clock, cin : IN STD_LOGIC := '0';
        add_sub                 : IN STD_LOGIC := '1';
        result : OUT STD_LOGIC_VECTOR(LPM_WIDTH-1 DOWNTO 0);
        cout, overflow          : OUT STD_LOGIC);
END COMPONENT;
```

## Ports

The following table displays all input ports of `lpm_add_sub`:

Port name	Required	Description	Comments
<code>cin</code>	No	Carry-in to the low-order bit. If the operation is ADD, low = 0 and high = +1. If the operation is SUB, low = -1 and high = 0.	If omitted, the default is 0 (i.e., low if the operation is ADD and high if the operation is SUB).
<code>dataa</code>	Yes	Augend/Minuend	Input port <code>LPM_WIDTH</code> wide
<code> datab</code>	Yes	Addend/Subtrahend	Input port <code>LPM_WIDTH</code> wide
<code>add_sub</code>	No	If the signal is high, the operation = <code>dataaa</code> + <code> datab</code> . If the signal is low, the operation = <code>dataaa</code> - <code> datab</code> .	If the <code>LPM_DIRECTION</code> parameter is used, <code>add_sub</code> cannot be used. If omitted, the default is ADD. Altera recommends that you use the <code>LPM_DIRECTION</code> parameter to specify the operation of the <code>lpm_add_sub</code> function, rather than assigning a constant to the <code>add_sub</code> port.
<code>clock</code>	No	Clock for pipelined usage	The clock port provides pipelined operation for the <code>lpm_add_sub</code> function. For <code>LPM_PIPELINE</code> values other than 0 (default value), the <code>clock</code> port must be connected.
<code>clken</code>	No	Clock enable for pipelined usage	Available for VHDL only
<code>aclr</code>	No	Asynchronous clear for pipelined usage	The pipeline initializes to an undefined (X) logic level. The <code>aclr</code> port can be used at any time to reset the pipeline to all 0s, asynchronously to the <code>clock</code> signal.

The following table displays all output ports of `lpm_add_sub`:

Port Name	Required	Description	Comments
<code>result</code>	Yes	<code>dataaa + or - datab</code> or <code>+ or - cin</code>	Output port <code>LPM_WIDTH</code> wide
<code>cout</code>	No	Carry-out (borrow-in) of the MSB	If <code>overflow</code> is used, <code>cout</code> cannot be used. The <code>cout</code> port has a physical interpretation as the carry-out (borrow-in) of the MSB. <code>cout</code> is most meaningful for detecting overflow in <code>UNSIGNED</code> operations.
<code>overflow</code>	No	Result exceeds available precision.	If <code>overflow</code> is used, <code>cout</code> cannot be used. The <code>overflow</code> port has a physical interpretation as the XOR of the carry-in to the MSB with the carry-out of the MSB. <code>overflow</code> is meaningful only when the <code>LPM REPRESENTATION</code> parameter value is <code>SIGNED</code> .

## Parameters

The following table shows the parameters of the `lpm_add_sub` component:

Parameter	Type	Required	Description
LPM_WIDTH	Integer	Yes	Width of the <code>dataa</code> , <code>datab</code> , and <code>result</code> ports.
LPM_DIRECTION	String	No	Values are <code>ADD</code> , <code>SUB</code> , and <code>UNUSED</code> . If omitted, the default is <code>DEFAULT</code> , which directs the parameter to take its value from the <code>add_sub</code> port. The <code>add_sub</code> port cannot be used if <code>LPM_DIRECTION</code> is used. Altera recommends that you use the <code>LPM_DIRECTION</code> parameter to specify the operation of the <code>lpm_add_sub</code> function, rather than assigning a constant to the <code>add_sub</code> port.
LPM REPRESENTATION	String	No	Type of addition performed: <code>SIGNED</code> , <code>UNSIGNED</code> , or <code>UNUSED</code> . If omitted, the default is <code>SIGNED</code> .
LPM_PIPELINE	Integer	No	Specifies the number of clock cycles of latency associated with the <code>result</code> output. A value of zero (0) indicates that no latency exists, and that a purely combinatorial function will be instantiated. If omitted, the default is 0 (nonpipelined).
LPM_HINT	String	No	Allows you to specify Altera-specific parameters in VHDL design files. The default is <code>UNUSED</code> .
LPM_TYPE	String	No	Identifies the LPM entity name in VHDL design files.
ONE_INPUT_IS_CONSTANT	String	No	Altera-specific parameter. Values are <code>YES</code> , <code>NO</code> , and <code>UNUSED</code> . Provides greater optimization, if one input is constant. If omitted, the default is <code>NO</code> .
MAXIMIZE_SPEED	Integer	No	Altera-specific parameter. You can specify a value between 0 and 10. If used, MaxPlus II attempts to optimize a specific instance of the <code>lpm_add_sub</code> function for speed rather than area, and overrides the setting of the Optimize option in the Global Project Logic Synthesis dialog box (Assign menu). If <code>MAXIMIZE_SPEED</code> is unused, the value of the Optimize option is used instead. If the setting for <code>MAXIMIZE_SPEED</code> is 6 or higher, the compiler will optimize <code>lpm_add_sub</code> megafunctions for higher speed; if the setting is 5 or less, the compiler will optimize for smaller area.

Note that for Verilog LPM 220 synthesizable code (i.e., `220model.v`) the following parameter ordering applies: `lpm_type`, `lpm_width`, `lpm_direction`, `lpm_representation`, `lpm_pipeline`, `lpm_hint`.

## Function

The following table is an example of the UNSIGNED behavior in `lpm_add_sub`:

Inputs			Outputs	
add_sub	dataa	datab	cout, result	overflow
1	a	b	$a + b + \text{cin}$	$\text{cout}$
0	a	b	$a - b - \text{cin}$	$!\text{cout}$

The following table is an example of the SIGNED behavior in `lpm_add_sub`:

Inputs			Outputs	
add_sub	dataa	datab	cout, sum	overflow
1	a	b	$a + b + \text{cin}$	$a \geq 0 \text{ and } b \geq 0$ and $\text{sum} < 0$ or $a < 0 \text{ and } b < 0 \text{ and }$ $\text{sum} \geq 0$
0	a	b	$a - b - \text{cin}$	$a \geq 0 \text{ and } b < 0$ and $\text{sum} < 0$ or $a < 0 \text{ and } b \geq 0$ and $\text{sum} \geq 0$

## Resource Usage

The following table summarizes the resource usage for an `lpm_add_sub` megafunction used to implement a 16-bit unsigned adder with a carry-in input and a carry-out output. Logic cell usage scales linearly in proportion to adder width.

Design goals		Design results		
Device family	Optimization	LEs	Speed (ns)	Notes
FLEX 6K, 8K, and 10K	Routability Speed	45 18	53 17	Speed for EPF8282A-2
MAX 5K, 7K, and 9K	Routability	28 (22)	23	Speed for EPM7128E-7

Numbers of shared expanders used are shown in parentheses.

### B.2.3 The Parameterized Multiplier Megafunction (`lpm_mult`)

Altera recommends that you use `lpm_mult` to replace all other types of multiplier functions, including old-style multiplier macrofunctions. We have used

this megafunction for the designs `fir_gen`, p. 167, `ccmul`, p. 368, `fir_lms`, p. 504, and `fir6dlms`, p. 511.

Altera recommends instantiating this function as described in “Using the MegaWizard Plug-In Manager” in the Quartus II help.

The port names and order for Verilog HDL prototype are:

```
module lpm_mult ( dataa, datab, sum, aclr, clock,
                   result);
```

The VHDL component declaration is shown below:

```
COMPONENT lpm_mult
  GENERIC (LPM_WIDTHA: POSITIVE;
           LPM_WIDTHB: POSITIVE;
           LPM_WIDTHS: POSITIVE;
           LPM_WIDTHP: POSITIVE;
           LPM REPRESENTATION: STRING := "UNSIGNED";
           LPM_PIPELINE: INTEGER := 0;
           LPM_TYPE: STRING := "L_MULT";
           LPM_HINT : STRING := "UNUSED");
  PORT (dataa : IN STD_LOGIC_VECTOR(LPM_WIDTHA-1 DOWNTO 0);
         datab : IN STD_LOGIC_VECTOR(LPM_WIDTHB-1 DOWNTO 0);
         aclr, clken, clock : IN STD_LOGIC := '0';
         sum    : IN STD_LOGIC_VECTOR(LPM_WIDTHS-1 DOWNTO 0)
                     := (OTHERS => '0');
         result: OUT STD_LOGIC_VECTOR(LPM_WIDTHP-1 DOWNTO 0)
                   );
  END COMPONENT;
```

## Ports

The following table displays all input ports of `lpm_mult`:

Port Name	Required	Description	Comments
<b>dataa</b>	Yes	Multiplicand	Input port LPM_WIDTHA wide
<b> datab</b>	Yes	Multiplier	Input port LPM_WIDTHB wide
<b>sum</b>	No	Partial sum	Input port LPM_WIDTHS wide
<b>clock</b>	No	Clock for pipelined usage	The <b>clock</b> port provides pipelined operation for the <b>lpm_mult</b> function. For <b>LPM_PIPELINE</b> values other than 0 (default value), the <b>clock</b> port must be connected.
<b>clken</b>	No	Clock enable for pipelined usage	Available for VHDL only.
<b>aclr</b>	No	Asynchronous clear for pipelined usage	The pipeline initializes to an undefined (X) logic level. The <b>aclr</b> port can be used at any time to reset the pipeline to all 0s, asynchronously to the <b>clock</b> signal.

The following table displays all output ports of **lpm\_mult**:

Port Name	Re- quired	Description	Comments
<b>result</b>	Yes	<code>result = dataa * datab + sum.</code> The product LSB is aligned with the sum LSB.	Output port LPM_WIDTHP wide. If <b>LPM_WIDTHP</b> < max ( <b>LPM_WIDTHA</b> + <b>LPM_WIDTHB</b> , <b>LPM_WIDTHS</b> ) or ( <b>LPM_WIDTHA</b> + <b>LPM_WIDTHS</b> ), only the <b>LPM_WIDTHP</b> MSBs are present.

## Parameters

The following table shows the parameters of the **lpm\_mult** component:

Parameter	Type	Required	Description
LPM_WIDTHA	Integer	Yes	Width of the <b>dataa</b> port
LPM_WIDTHB	Integer	Yes	Width of the <b>datab</b> port
LPM_WIDTHP	Integer	Yes	Width of the <b>result</b> port
LPM_WIDTHS	Integer	Yes	Width of the <b>sum</b> port. Required even if the <b>sum</b> port is not used.
LPM REPRESENTATION	String	No	Type of multiplication performed: <b>SIGNED</b> , <b>UNSIGNED</b> , or <b>UNUSED</b> . If omitted, the default is <b>UNSIGNED</b> .
LPM_PIPELINE	Integer	No	Specifies the number of clock cycles of latency associated with the <b>result</b> output. A value of zero (0) indicates that no latency exists, and that a purely combinatorial function will be instantiated. If omitted, the default is 0 (non-pipelined).
LPM_HINT	String	No	Allows you to assign Altera-specific parameters in VHDL design files. The default is <b>UNUSED</b> .
LPM_TYPE	String	No	Identifies the LPM entity name in VHDL design files.
INPUT_A_IS_CONSTANT	String	No	Altera-specific parameter. Values are <b>YES</b> , <b>NO</b> , and <b>UNUSED</b> . If <b>dataa</b> is connected to a constant value, setting <b>INPUT_A_IS_CONSTANT</b> to <b>YES</b> optimizes the multiplier for resource usage and speed. If omitted, the default is <b>NO</b> .
INPUT_B_IS_CONSTANT	String	No	Altera-specific parameter. Values are <b>YES</b> , <b>NO</b> , and <b>UNUSED</b> . If <b>datab</b> is connected to a constant value, setting <b>INPUT_B_IS_CONSTANT</b> to <b>YES</b> optimizes the multiplier for resource usage and speed. The default is <b>NO</b> .

Parameter	Type	Required	Description
USE_EAB	String	No	Altera-specific parameter. Values are ON, OFF, and UNUSED. Setting the USE_EAB parameter to ON allows Quartus II to use EABs to implement $4 \times 4$ or $(8 \times \text{constant value})$ building blocks in FLEX 10K devices. Altera recommends that you set USE_EAB to ON only when LCELLS are in short supply. If you wish to use this parameter, when you instantiate the function in a GDF, you must specify it by entering the parameter name and value manually with the Edit Ports/Parameters dialog box (Symbol menu). You can also use this parameter name in a TDF or a Verilog design file. You must use the LPM_HINT parameter to specify the USE_EAB parameter in VHDL design files.
DEDICATED_MULTIPLIER_CIRCUITRY	String	No	Altera-specific parameter. You must use the LPM_HINT parameter to specify the DEDICATED_MULTIPLIER_CIRCUITRY parameter in VHDL design files. Specifies whether to use dedicated multiplier circuitry. Values are ‘AUTO’, YES, and ‘NO’. If omitted, the default is AUTO.
LATENCY	Integer	No	Altera-specific parameter. Same as LPM_PIPELINE. (This parameter is provided only for backward compatibility with MaxPlus II pre-version 7.0 designs. For all new designs, you should use the LPM_PIPELINE parameter instead.)
MAXIMIZE_SPEED	Integer	No	Altera-specific parameter. You can specify a value between 0 and 10. If used, MaxPlus II attempts to optimize a specific instance of the lpm_mult function for speed rather than area, and overrides the setting of the Optimize option in the Global Project Logic Synthesis dialog box (Assign menu). If MAXIMIZE_SPEED is unused, the value of the Optimize option is used instead. If the setting for MAXIMIZE_SPEED is 6 or higher, the compiler will optimize lpm_mult megafunctions for higher speed; if the setting is 5 or less, the compiler will optimize for smaller area.
LPM_HINT	String	No	Allows you to specify Altera-specific parameters in VHDL design files. The default is UNUSED.

Note that specifying a value for MAXIMIZE\_SPEED has an effect only if LPM REPRESENTATION is set to SIGNED.

Note that for Verilog LPM 220 synthesizable code (i.e., 220model.v) the following parameter ordering applies: lpm\_type, lpm\_widtha, lpm\_widthb, lpm\_widths, lpm\_widthp, lpm\_representation, lpm\_pipeline, lpm\_hint.

## Function

The following table is an example of the UNSIGNED behavior in `lpm_mult`:

Inputs			Outputs
dataa datab sum			product
a	b	s	LPM_WIDTHP most significant bits of $a * b + s$

## Resource Usage

The following table summarizes the resource usage for an `lpm_mult` function used to implement 4-bit and 8-bit multipliers with `LPM_PIPELINE = 0` and without the optional `sum` input. Logic cell usage scales linearly in proportion to the square of the input width.

Design goals		Design results			
Device family	Optimization	Width	LEs	Speed (ns)	Notes
FLEX 6K, 8K, and 10K	Routability	8	121	80	Speed for EPF8282A-2
	Speed	8	163	52	
FLEX 6K, 8K, and 10K	Routability	4	29	34	Speed for EPF8282A-2
	Speed	4	41	27	
MAX 5K, 7K, and 9K	Routability	4	26 (11)	23	Speed for EPM7128E-7
	Speed	4	27 (4)	19	

Numbers of shared expanders used are shown in parentheses. In the FLEX 10K device family, the 4-bit by 4-bit multiplier example shown above can be implemented in a single EAB.

### B.2.4 The Parameterized ROM Megafunction (`lpm_rom`)

The `lpm_rom` block is parameterized ROM with separate input and output clocks. We have used this megafunction for the designs `fun_text`, p. 30 and `darom`, p. 196.

The `lpm_rom` block can also be used with older device families, e.g., Flex 10K. Altera translates for newer devices like Cyclone II the `lpm_rom` in the `altsyncram` megafunction block. But the `altsyncram` is not supported for Flex 10K that is used on the popular UP2 boards.

Altera recommends instantiating this function as described in “Using the MegaWizard Plug-In Manager” in the Quartus II help.

The port names and order for Verilog HDL prototype are:

```
module lpm_rom ( address, inclock, outclock, memenab,
                 q);
```

The VHDL component declaration is shown below:

```
COMPONENT lpm_rom
  GENERIC (LPM_WIDTH      : POSITIVE;
           LPM_TYPE       : STRING := "L_ROM";
           LPM_WIDTHAD   : POSITIVE;
           LPM_NUMWORDS  : POSITIVE;
           LPM_FILE       : STRING;
           LPM_ADDRESS_CONTROL : STRING := "REGISTERED";
           LPM_OUTDATA    : STRING := "REGISTERED";
           LPM_HINT       : STRING := "UNUSED");
  PORT(address : IN STD_LOGIC_VECTOR(LPM_WIDTHAD-1 DOWNTO 0);
        inclock : IN STD_LOGIC := '1';
        outclock : IN STD_LOGIC := '1';
        memenab  : IN STD_LOGIC := '1';
        q        : OUT STD_LOGIC_VECTOR(LPM_WIDTH-1 DOWNTO 0)
      );
END COMPONENT;
```

## Ports

The following table displays all input ports of `lpm_rom`:

Port name	Re- quired	Description	Comments
<code>address</code>	Yes	Address input to the memory	Input port <code>LPM_WIDTHAD</code> wide
<code>inclock</code>	No	Clock for input registers	The <code>address</code> port is synchronous (registered) when the <code>inclock</code> port is connected, and is asynchronous (registered) when the <code>inclock</code> port is not connected.
<code>outclock</code>	No	Clock for output registers	The addressed memory content-to-q response is synchronous when the <code>outclock</code> port is connected, and is asynchronous when it is not connected.
<code>memenab</code>	No	Memory enable input	High = data output on <code>q</code> , Low = high-impedance outputs

The following table displays all output ports of `lpm_rom`:

Port Name	Re- quired	Description	Comments
<code>q</code>	Yes	Output of memory	Output port <code>LPM_WIDTH</code> wide

## Parameters

The following table shows the parameters of the `lpm_rom` component:

Parameter	Type	Required	Description
<code>LPM_WIDTH</code>	Integer	Yes	Width of the <code>q</code> port.
<code>LPM_WIDTHAD</code>	Integer	Yes	Width of the <code>address</code> port. <code>LPM_WIDTHAD</code> should be (but is not required to be) equal to $\log_2(\text{LPM_NUMWORDS})$ . If <code>LPM_WIDTHAD</code> is too small, some memory locations will not be addressable. If it is too large, addresses that are too high will return undefined logic levels.
<code>LPM_NUMWORDS</code>	Integer	Yes	Number of words stored in memory. In general, this value should be (but is not required to be) $2^{\text{LPM\_WIDTHAD}} - 1 < \text{LPM\_NUMWORDS} \leq 2^{\text{LPM\_WIDTHAD}}$ . If omitted, the default is $2^{\text{LPM\_WIDTHAD}}$ .
<code>LPM_FILE</code>	String	No	Name of the Memory Initialization File (*.mif) or Hexadecimal (Intel-format) File (*.hex) containing ROM initialization data (<filename>), or <code>UNUSED</code> .
<code>LPM_ADDRESS_CONTROL</code>	String	No	Values are <code>REGISTERED</code> , <code>UNREGISTERED</code> , and <code>UNUSED</code> . Indicates whether the address port is registered. If omitted, the default is <code>REGISTERED</code> .
<code>LPM_OUTDATA</code>	String	No	Values are <code>REGISTERED</code> , <code>UNREGISTERED</code> , and <code>UNUSED</code> . Indicates whether the <code>q</code> and <code>eq</code> ports are registered. If omitted, the default is <code>REGISTERED</code> .
<code>LPM_HINT</code>	String	No	Allows you to specify Altera-specific parameters in VHDL design files. The default is <code>UNUSED</code> .
<code>LPM_TYPE</code>	String	No	Identifies the LPM entity name in VHDL design files.

Note that for Verilog LPM 220 synthesizable code (i.e., `220model.v`) the following parameter ordering applies: `lpm_type`, `lpm_width`, `lpm_widthad`, `lpm_numwords`, `lpm_address_control`, `lpm_outdata`, `lpm_file`, `lpm_hint`.

## Function

The following table shows the *synchronous* read from memory behavior of `lpm_rom`:

OUTCLOCK	MEMENAB	Function
X	L	q output is high impedance (memory not enabled)
1	H	No change in output
Z	H	The output register is loaded with the contents of the memory location pointed to by <code>address</code> . q outputs the contents of the output register.

The output `q` is asynchronous and reflects the data in the memory to which `address` points. The following table shows the *asynchronous* memory operations behavior of `lpm_rom`:

MEMENAB	Function
L	q output is high-impedance (memory not enabled)
H	The memory location pointed to by <code>address</code> is read

Totally asynchronous memory operations occur when neither `inclock` nor `outclock` is connected. The output `q` is asynchronous and reflects the memory location pointed to by `address`. Since this totally asynchronous memory operation is only available with Flex 10K devices, but not with Cyclone II, we do not use this mode in our designs. Either input or output is registered in all of our designs that use memory blocks.

## Resource Usage

The Megafunction `lpm_rom` uses one embedded cell per memory bit.

### B.2.5 The Parameterized Divider Megafunction (`lpm_divide`)

Altera recommends that you use `lpm_divide` to replace all other types of divider functions, including old-style divide macrofunction. We have used this megafunction for the array divider designs p. 103.

Altera recommends instantiating this function as described in “Using the MegaWizard Plug-In Manager” in the Quartus II help.

The port names and order for Verilog HDL prototype are:

```
module lpm_divide ( quotient, remain, numer, denom,
                     clock, clken, aclr )
```

The VHDL component declaration is shown below:

```
COMPONENT lpm_divide
  GENERIC ( LPM_WIDTHN: POSITIVE;
            LPM_WIDTHD: POSITIVE;
            LPM_NREPRESENTATION: STRING := "UNSIGNED";
            LPM_DREPRESENTATION: STRING := "UNSIGNED";
            LPM_TYPE: STRING := "LPM_DIVIDE";
```

```

        LPM_PIPELINE: INTEGER := 0;
        LPM_HINT: STRING:= "UNUSED";
    );
PORT  ( numer: IN STD_LOGIC_VECTOR(LPM_WIDTHN-1 DOWNTO 0);
        denom: IN STD_LOGIC_VECTOR(LPM_WIDTHD-1 DOWNTO 0);
        clock, aclr: IN STD_LOGIC := '0';
        clken: IN STD_LOGIC := '1';
        quotient: OUT STD_LOGIC_VECTOR(LPM_WIDTHN-1 DOWNTO 0);
        remain: OUT STD_LOGIC_VECTOR(LPM_WIDTHD-1 DOWNTO 0)
    );
END COMPONENT;

```

## Ports

The following table displays all input ports of `lpm_divide`:

Port Name	Required	Description	Comments
<code>numer</code>	Yes	Numerator	Input port <code>LPM_WIDTHN</code> wide.
<code>denom</code>	Yes	Denominator	Input port <code>LPM_WIDTHD</code> wide.
<code>clock</code>	No	Clock input for pipelined usage.	You must connect the <code>clock</code> input if you set <code>LPM_PIPELINE</code> to a value other than 0.
<code>clken</code>	No	Clock enable for pipelined usage.	
<code>aclr</code>	No	Asynchronous clear signal.	The <code>aclr</code> port may be used at any time to reset the pipeline to all 0s asynchronously to the <code>clock</code> input.

The following table displays all output ports of `lpm_divide`:

Port Name	Required	Description	Comments
<code>quotient</code>	Yes	Output port <code>LPM_WIDTHN</code> wide.	You must use either the <code>quotient</code> or the <code>remain</code> ports.
<code>remain</code>	Yes	Output port <code>LPM_WIDTHD</code> wide.	You must use either the <code>quotient</code> or the <code>remain</code> ports.

## Parameters

The following table shows the parameters of the `lpm_divide` component:

Parameter	Type	Required	Description
<code>LPM_WIDTHN</code>	Integer	Yes	Width of the <code>numer</code> and <code>quotient</code> port
<code>LPM_WIDTHD</code>	Integer	Yes	Width of the <code>denom</code> and <code>remain</code> port
<code>LPM_NREPRESENTATION</code>	String	No	Specifies whether the numerator is <code>SIGNED</code> or <code>UNSIGNED</code> . Only <code>UNSIGNED</code> is supported for now.
<code>LPM_DREPRESENTATION</code>	String	No	Specifies whether the denominator is <code>SIGNED</code> or <code>UNSIGNED</code> . Only <code>UNSIGNED</code> is supported for now.
<code>LPM_PIPELINE</code>	Integer	No	Specifies the number of clock cycles of latency associated with the <code>quotient</code> and <code>remain</code> outputs. A value of zero (0) indicates that no latency exists, and that a purely combinatorial function will be instantiated. If omitted, the default is 0 (nonpipelined). You cannot specify a value for the <code>LPM_PIPELINE</code> parameter that is higher than <code>LPM_WIDTHN</code> .
<code>LPM_TYPE</code>	String	No	Identifies the LPM entity name in VHDL design files.
<code>LPM_HINT</code>	String	No	Allows you to assign Altera-specific parameters in VHDL design files. The default is <code>UNUSED</code> .

You can pipeline a design by connecting the `clock` input and specifying the number of clock cycles of latency with the `LPM_PIPELINE` parameter.

Note that for Verilog LPM 220 synthesizable code (i.e., `220model.v`) the following parameter ordering applies: `lpm_type`, `lpm_widthn`, `lpm_widthd`, `lpm_nrepresentation`, `lpm_drepresentation`, `lpm_pipeline`.

### B.2.6 The Parameterized RAM Megafunction (`lpm_ram_dq`)

The `lpm_ram_dq` block is parameterized RAM with separate input and output ports. The `lpm_ram_dq` block can also be used with older device families, e.g., Flex10K. Altera translates for newer devices like Cyclone II the `lpm_ram_dq` in the `altsyncram` megafunction block. But the `altsyncram` is not supported for Flex10K that is used on the popular UP2 boards.

We have used this megafunction for the design `trisc0`, p. 606.

Altera recommends instantiating this function as described in “Using the MegaWizard Plug-In Manager” in the Quartus II help.

The port names and order for Verilog HDL prototype are:

```
module lpm_ram_dq ( q, data, inclock, outclock, we, address);
```

The VHDL component declaration is shown below:

```

COMPONENT lpm_ram_dq
  GENERIC
    LPM_WIDTH          : POSITIVE;
    LPM_WIDTHAD        : POSITIVE;
    LPM_NUMWORDS       : NATURAL := 0;
    LPM_INDATA         : STRING  := "REGISTERED";
    LPM_ADDRESS_CONTROL: STRING  := "REGISTERED";
    LPM_OUTDATA        : STRING  := "REGISTERED";
    LPM_FILE           : STRING  := "UNUSED";
    LPM_TYPE           : STRING  := "LPM_RAM_DQ";
    LPM_HINT           : STRING  := "UNUSED" );
  PORT
    (data : IN STD_LOGIC_VECTOR(LPM_WIDTH-1 DOWNTO 0);
     address : IN STD_LOGIC_VECTOR(LPM_WIDTHAD-1 DOWNTO 0);
     inclock, outclock : IN STD_LOGIC := '0';
     we : IN STD_LOGIC;
     q : OUT STD_LOGIC_VECTOR(LPM_WIDTH-1 DOWNTO 0)
    );
END COMPONENT;

```

## Ports

The following table displays all input ports of `lpm_ram_dq`:

Port Name	Required	Description	Comments
address	Yes	Address input to the memory	Input port LPM_WIDTHAD wide
data	Yes	Data input to the memory	Input port LPM_WIDTHAD wide
inclock	No	Clock for input registers	The <code>address</code> port is synchronous (registered) when the <code>inclock</code> port is connected, and is asynchronous (registered) when the <code>inclock</code> port is not connected.
outclock	No	Clock for output registers	The addressed memory content-to-q response is synchronous when the <code>outclock</code> port is connected, and is asynchronous when it is not connected.
we	Yes	Memory enable input	Write enable input. Enables write operations to the memory when high.

The following table displays all output ports of `lpm_ram_dq`:

Port Name	Required	Description	Comments
q	Yes	Output of memory	Output port LPM_WIDTH wide

## Parameters

The following table shows the parameters of the `lpm_ram_dq` component:

Parameter	Type	Required	Description
<code>LPM_WIDTH</code>	Integer	Yes	Width of the <code>q</code> port.
<code>LPM_WIDTHAD</code>	Integer	Yes	Width of the address port. <code>LPM_WIDTHAD</code> should be (but is not required to be) equal to $\log_2(\text{LPM_NUMWORDS})$ . If <code>LPM_WIDTHAD</code> is too small, some memory locations will not be addressable. If it is too large, addresses that are too high will return undefined logic levels.
<code>LPM_NUMWORDS</code>	Integer	Yes	Number of words stored in memory. In general, this value should be (but is not required to be) $2^{\text{LPM\_WIDTHAD}} - 1 < \text{LPM\_NUMWORDS} \leq 2^{\text{LPM\_WIDTHAD}}$ . If omitted, the default is $2^{\text{LPM\_WIDTHAD}}$ .
<code>LPM_FILE</code>	String	No	Name of the Memory Initialization File (*.mif) or Hexadecimal (Intel-format) File (*.hex) containing ROM initialization data (<filename>), or <code>UNUSED</code> .
<code>LPM_ADDRESS_CONTROL</code>	String	No	Values are <code>REGISTERED</code> , <code>UNREGISTERED</code> , and <code>UNUSED</code> . Indicates whether the address port is registered. If omitted, the default is <code>REGISTERED</code> .
<code>LPM_OUTDATA</code>	String	No	Values are <code>REGISTERED</code> , <code>UNREGISTERED</code> , and <code>UNUSED</code> . Indicates whether the <code>q</code> and <code>eq</code> ports are registered. If omitted, the default is <code>REGISTERED</code> .
<code>LPM_HINT</code>	String	No	Allows you to specify Altera-specific parameters in VHDL design files. The default is <code>UNUSED</code> .
<code>LPM_TYPE</code>	String	No	Identifies the LPM entity name in the VHDL design files.

Note that for Verilog LPM 220 synthesizable code (i.e., `220model.v`) the following parameter ordering applies: `lpm_type`, `lpm_width`, `lpm_widthad`, `lpm_numwords`, `lpm_address_control`, `lpm_outdata`, `lpm_file`, `lpm_hint`.

## Function

The following table shows the *synchronous* read and write memory behavior of `lpm_ram_dq`:

<code>inclock</code>	<code>we</code>	Function
X	-	No change (requires rising clock edge).
J	H	The memory location pointed to by <code>address</code> is loaded with <code>data</code> .
J	L	The memory location pointed to by <code>address</code> is read from the array. If <code>outclock</code> is not used, the read data appears at the outputs.

The following table shows the synchronous read from memory from memory operations behavior of `lpm_ram_dq`:

<code>outclock</code>	Function
-	No change
J	The memory location pointed to by <code>address</code> is read and written into the output register.

Totally asynchronous memory operations occur when neither `inclock` nor `outclock` is connected. The output `q` is asynchronous and reflects the memory location pointed to by `address`. Since this totally asynchronous memory operation is only available with Flex 10K devices, but not with Cyclone II, we do not use this mode in our designs. Either the input or output is registered in all of our designs that use memory blocks.

## Resource Usage

The Megafunction `lpm_ram_dq` uses one embedded cell per memory bit.

## C. Glossary

ACC	Accumulator
ACT	Actel FPGA family
ADC	Analog-to-digital converter
ADCL	All-digital CL
ADF	Adaptive digital filter
ADPCM	Adaptive differential pulse code modulation
ADPLL	All-digital PLL
ADSP	Analog Devices digital signal processor family
AES	Advanced encryption standard
AFT	Arithmetic Fourier transform
AHDL	Altera HDL
AHSM	Additive half square multiplier
ALU	Arithmetic logic unit
AM	Amplitude modulation
AMBA	Advanced microprocessor bus architecture
AMD	Advanced Micro Devices, Inc.
ASCII	American standard code for information interchange
ASIC	Application-specific IC
AWGN	Additive white Gaussian noise
BCD	Binary coded decimal
BDD	Binary decision diagram
BLMS	Block LMS
BP	Bandpass
BRS	Base removal scaling
BS	Barrelshifter
CAE	Computer-aided engineering
CAM	Content addressable memory
CAST	Carlisle Adams and Stafford Tavares
CBC	Cipher block chaining
CBIC	Cell-based IC
CD	Compact disc
CFA	Common factor algorithm
CFB	Cipher feedback
CIC	Cascaded integrator comb
CISC	Complex instruction set computer
CL	Costas loop
CLB	Configurable logic block
C-MOMS	Causal MOMS

CMOS	Complementary metal oxide semiconductor
CODEC	Coder/decoder
CORDIC	Coordinate rotation digital computer
COTS	Commercial off-the-shelf technology
CPLD	Complex PLD
CPU	Central processing unit
CQF	Conjugate quadrature filter
CRNS	Complex RNS
CRT	Chinese remainder theorem
CSOC	Canonical self-orthogonal code
CSD	Canonical signed digit
CWT	Continuous wavelet transform
CZT	Chirp- $z$ transform
DA	Distributed arithmetic
DAC	Digital-to-analog converter
DAT	Digital audio tap
DB	Daubechies filter
DC	Direct current
DCO	Digital controlled oscillator
DCT	Discrete cosine transform
DCU	Data cache unit
DES	Data encryption standard
DFT	Discrete Fourier transform
DHT	Discrete Hartley transform
DIF	Decimation in frequency
DIT	Decimation in time
DLMS	Delayed LMS
DMA	Direct memory access
DMIPS	Dhrystone MIPS
DMT	Discrete Morlet transform
DPLL	Digital PLL
DSP	Digital signal processing
DST	Discrete sine transform
DWT	Discrete wavelet transform
EAB	Embedded array block
ECB	Electronic code book
ECL	Emitter coupled logic
EDIF	Electronic design interchange format
EFF	Electronic Frontier Foundation
EPF	Altera FPGA family
EPROM	Electrically programmable ROM
ERA	Plessey FPGA family
ERNS	Eisenstein RNS
ESA	European Space Agency
EVR	Eigenvalue ratio
EXU	Execution unit
FAEST	Fast a posteriori error sequential technique
FCT	Fast cosine transform
FC2	FPGA compiler II
FF	Flip-flop

FFT	Fast Fourier transform
FIFO	First-in first-out
FIR	Finite impulse response
FIT	Fused internal timer
FLEX	Altera FPGA family
FM	Frequency modulation
FNT	Fermat NTT
FPGA	Field-programmable gate array
FPL	Field-programmable logic (combines CPLD and FPGA)
FPLD	FPL device
FSF	Frequency sampling filter
FSK	Frequency shift keying
FSM	Finite state machine
GAL	Generic array logic
GF	Galois field
GNU	GNU's not Unix
GPP	General-purpose processor
GPR	General-purpose register
HB	Half-band filter
HI	High frequency
HDL	Hardware description language
HSP	Harris Semiconductor DSP ICs
IBM	International Business Machines (corporation)
IC	Integrated circuit
ICU	Instruction cache unit
IDCT	Inverse DCT
IDEA	International data encryption algorithm
IDFT	Inverse discrete Fourier transform
IEEE	Institute of Electrical and Electronics Engineers
IF	Inter frequency
IFFT	Inverse fast Fourier transform
IIR	Infinite impulse response
I-MOMS	Interpolating MOMS
INTT	Inverse NTT
IP	Intellectual property
I/Q	In-/Quadrature phase
ISA	Instruction set architecture
ITU	International Telecommunication Union
JPEG	Joint photographic experts group
JTAG	Joint test action group
KCPSM	Ken Chapman PSM
KLT	Karhunen–Loeve transform
LAB	Logic array block
LAN	Local area network
LC	Logic cell
LE	Logic element
LIFO	Last-in first-out

LISA	Language for instruction set architecture
LF	Low frequency
LFSR	Linear feedback shift register
LMS	Least-mean-square
LNS	Logarithmic number system
LO	Low frequency
LP	Lowpass
LPM	Library of parameterized modules
LRS	Serial left right shifter
LS	Least-square
LSB	Least-significant bit
LSI	Large scale integration
LTI	Linear time-invariant
LUT	Look-up table
MAC	Multiplication and accumulate
MACH	AMD/Vantis FPGA family
MAG	Multiplier adder graph
MAX	Altera CPLD family
MIF	Memory initialization file
MIPS	Microprocessor without interlocked pipeline
MIPS	Million instructions per second
MLSE	Maximum-likelihood sequence estimator
MMU	Memory management unit
MMX	Multimedia extension
MNT	Mersenne NTT
MOMS	Maximum order minimum support
$\mu$ P	Microprocessor
MPEG	Moving Picture Experts Group
MPX	Multiplexer
MSPS	Millions of sample per second
MRC	Mixed radix conversion
MSB	Most significant bit
MUL	Multiplication
NCO	Numeric controlled oscillators
NLMS	Normalized LMS
NP	Nonpolynomial complex problem
NRE	Nonrecurring engineering costs
NTT	Number theoretic transform
OFB	Open feedback (mode)
O-MOMS	Optimal MOMS
PAM	Pulse-amplitude modulated
PC	Personal computer
PCI	Peripheral component interconnect
PD	Phase detector
PDSP	Programmable digital signal processor
PFA	Prime factor algorithm
PIT	Programmable interval timer
PLA	Programmable logic array
PLD	Programmable logic device

PLL	Phase-locked loop
PM	Phase modulation
PREP	Programmable Electronic Performance (cooperation)
PRNS	Polynomial RNS
PROM	Programmable ROM
PSK	Phase shift keying
PSM	Programmable state machine
QDFT	Quantized DFT
QLI	Quick look-in
QFFT	Quantized FFT
QMF	Quadrature mirror filter
QRNS	Quadratic RNS
QSM	Quarter square multiplier
RAM	Random-access memory
RC	Resistor/capacity
RF	Radio frequency
RISC	Reduced instruction set computer
RLS	Recursive least square
RNS	Residue number system
ROM	Read-only memory
RPFA	Rader prime factor algorithm
RS	Serial right shifter
RSA	Rivest, Shamir, and Adelman
SD	Signed digit
SG	Stochastic gradient
SIMD	Single instruction multiple data
SLMS	Signed LMS
SM	Signed magnitude
SNR	Signal-to-noise ratio
SPEC	System performance evaluation cooperation
SPLD	Simple PLD
SPT	Signed power-of-two
SR	Shift register
SRAM	Static random-access memory
SSE	Streaming SIMD extension
STFT	Short-term Fourier transform
TDLMS	Transform-domain LMS
TLB	Translation look-aside buffer
TLU	Table look-up
TMS	Texas Instruments DSP family
TI	Texas Instruments
TOS	Top of stack
TTL	Transistor transistor logic
TVP	True vector processor
UART	Universal asynchronous receiver/transmitter
VCO	Voltage-control oscillator
VHDL	VHSIC hardware description language

VHSIC	Very-high-speed integrated circuit
VLIW	Very long instruction word
VLSI	Very large integrated ICs
WDT	Watchdog timer
WFTA	Winograd Fourier transform algorithm
WSS	Wide sense stationary
XC	Xilinx FPGA family
XNOR	Exclusive NOR gate
YACC	Yet another compiler-compiler

## D. CD-ROM File: “1readme.ps”

The accompanying CD-ROM includes

- A full version of the Quartus II software
- Altera datasheets for Cyclone II devices
- All VHDL/Verilog design examples and utility programs and files

To install the Quartus II 6.0 web edition software first read the licence agreement carefully. Since the Quartus II 6.0 web edition software uses many other tools (e.g., GNU, Berkeley Tools, SUN microsystems tool, etc.) you need to agree to their licence agreements too before installing the software. To install the software start the self-extracting file `quartusii_60_web_edition.exe` on the CD-ROM in the `Altera` folder. After the installation the user must register the software through Altera's web page at [www.altera.com](http://www.altera.com) in order to get a permanent licence key. Otherwise the temporary licence key expires after the 30-day grace period and the software will no longer run. Altera frequently update the Quartus II software to support new devices and you may consider downloading the latest Quartus II version from the Altera webpage directly, but keep in mind that the files are large and that the synthesis results will differ slightly for another version. Altera's University program now delivers the files via download, which can take long time with a 56 Kbit/s MODEM.

The design examples for the book are located in the directories `book3e/vhdl` and `book3e/verilog` for the VHDL and Verilog examples, respectively. These directories contain, for each example, the following four files:

- The VHDL or Verilog source code (`*.vhd` and `*.v`)
- The Quartus project files (`*.qpf`)
- The Quartus setting files (`*.qsf`)
- The Simulator wave form file (`*.vwf`)

For the design `fun_graf`, the block design file (`*.bdf`) is included in `book3e/vhdl`. For the examples that utilize M4Ks (i.e., `fun_text`, `darom`, and `trisc0`), the memory initialization file (`*.mif`) can be found on the CD-ROM. To simplify the compilation and postprocessing, the source code directories include the additional (`*.bat`) files and Tcl scripts shown below:

File	Comment
qvhd1.tcl	Tcl script to compile all design examples. Note that the device can be changed from Cyclone II to Flex, Apex or Stratix just by changing the comment sign # in column 1 of the script.
qclean.bat	Cleans all temporary Quartus II compiler files, but not the report files (*.map.rpt), the timing analyzer output files (*.tan.rpt), and the project files *.qpf and *.qsf.
qveryclean.bat	Cleans all temporary compiler files, <i>including</i> all report files (*.rep) and project files.

Use the DOS prompt and type

```
quartus_sh -t qvhdl.tcl > qvhdl.txt
```

to compile all design examples and then **qclean.bat** to remove the unnecessary files. The Tcl script **qvhd1.tcl** is included on the CD. The Tcl script language developed by the Berkeley Professor John Ousterhout [346, 347, 348] (used by most modern CAD tools: Altera Quartus, Xilinx ISE, ModelTech, etc.) allows a comfortable scripting language to define setting, specify functions, etc. Given the fact that many tools also use the graphic toolbox Tcl/Tk we have witnessed that many tools now also looks almost the same.

Two search procedures (**show\_fmax** and **show\_resources**) are used within the Tcl script **qvhd1.tcl** to display resources and Registered Performance. The script includes all settings and also alternative device definitions. The protocol file **qvhd1.txt** has all the useful synthesis data. For the trisc0 processor, for instance, the list for the Cyclone II device EP2C35F672C6 is:

```
....  
-----  
trisc0 fmax: 115.65 MHz ( period = 8.647 ns )  
trisc0 LEs: 198 / 33,216 ( < 1 % )  
trisc0 M4K bits: 5,120 / 483,840 ( 1 % )  
trisc0 DSP blocks: 1 / 70 ( 1 % )  
-----  
....
```

The results for all examples are summarized in Table B.1, p. 731.

Other devices are prespecified and include the EPF10K20RC240-4 and EPF10K70RC240-4 from the UP1 and UP2 University boards, the EP20K200EFC484-2X from the Nios development boards, and three devices from other DSP boards available from Altera, i.e., the EP1S10F484C5, EP1S25F780C5, and EP2S60F1020C4ES.

## Using Compilers Other Then Quartus II

### Synopsys FPGA-CompilerII

The main advantage of using the FPGA-CompilerII (FC2) from Synopsys was that it was possible to synthesize examples for other devices like Xilinx, Vantis, Actel, or QuickLogic with the same tool. The Tcl scripts **vhd1.fc2**, and **verilog.fc2**,

respectively, were provided the necessary commands for the shell mode of FC2, i.e., `fc2_shell` in the second edition of the book [57]. Synopsys, however, since 2006 no longer supports the `FPGA_CompilerII` and it is therefore not a good idea to use the compiler anymore since the newer devices can not be selected.

## Model Technology

By using the synthesizable public-domain models provided by the EDIF organization (at [www.edif.org](http://www.edif.org)), it is also possible to use other VHDL/Verilog simulators than Quartus II.

**Using MTI and VHDL.** For VHDL, the two files `220pack.vhd` and `220model.vhd` must first be compiled. For the ModelSim simulator `vsim` from Model Technology Inc., the script `mti_vhdl.do` can be used for device-independent compilation and simulation of the design examples. The script is shown below:

```
#-----
# Model Technology VHDL compiler script for the book
# Digital Signal Processing with FPGAs (3.edition)
# Author-EMAIL: Uwe.Meyer-Baese@ieee.org
#-----

echo Create Library directory lpm
vlib lpm

echo Compile lpm package.
vcom -work lpm -explicit -quiet 220pack.vhd 220model.vhd

echo Compile chapter 1 entitys.
vcom -work lpm -quiet example.vhd fun_text.vhd

echo Compile chapter 2 entitys.
vcom -work lpm -explicit -quiet add1p.vhd add2p.vhd
vcom -work lpm -explicit -quiet add3p.vhd mul_ser.vhd
vcom -work lpm -explicit -quiet cordic.vhd

echo Compile chapter 3 components.
vcom -work lpm -explicit -quiet case3.vhd case5p.vhd
vcom -work lpm -explicit -quiet case3s.vhd
echo Compile chapter 3 entitys.
vcom -work lpm -explicit -quiet fir_gen.vhd fir_srg.vhd
vcom -work lpm -explicit -quiet dafsm.vhd darom.vhd
vcom -work lpm -explicit -quiet dasign.vhd dapara.vhd

echo Compile chapter 4 entitys.
vcom -work lpm -explicit -quiet iir.vhd iir_pipe.vhd
vcom -work lpm -explicit -quiet iir_par.vhd

echo Compile chapter 5 entitys.
vcom -work lpm -explicit -quiet cic3r32.vhd cic3s32.vhd
vcom -work lpm -explicit -quiet db4poly.vhd db4latti.vhd

echo Compile chapter 6 entitys.
```

```
vcom -work lpm -explicit -quiet rader7.vhd ccmul.vhd
vcom -work lpm -explicit -quiet bfproc.vhd

echo Compile chapter 7 entitys.
vcom -work lpm -explicit -quiet rader7.vhd ccmul.vhd
vcom -work lpm -explicit -quiet bfproc.vhd

echo Compile 2. edition entitys.
vcom -work lpm -explicit -quiet div_res.vhd div_aegp.vhd
vcom -work lpm -explicit -quiet fir_lms.vhd fir6dlms.vhd

echo Compile 3. edition entitys from chapter 2.
vcom -work lpm -explicit -quiet cmul7p8.vhd arctan.vhd
vcom -work lpm -explicit -quiet ln.vhd sqrt.vhd

echo Compile 3. edition entitys from chapter 5.
vcom -work lpm -explicit -quiet rc_sinc.vhd farrow.vhd
vcom -work lpm -explicit -quiet cmoms.vhd

echo Compile 3. edition entitys from chapter 9.
vcom -work lpm -explicit -quiet reg_file.vhd trisc0.vhd
```

Start the ModelSim simulator and then type

```
do mti_vhdl.do
```

to execute the script.

**Using MTI and Verilog.** Using the Verilog interface with the `lpm` library from EDIF, i.e., `220model.v`, needs some additional effort. When using `220model.v` it is necessary to specify *all* ports in the Verilog `lpm` components. There is an extra directory `book3e/verilog/mti`, which provides the design examples with a full set of `lpm` port specifications. The designs use

```
'\include "220model.v"
```

at the beginning of each Verilog file to include the `lpm` components, if necessary. Use the script `mti_v1.csh` and `mti_v2.csh` to compile all Verilog design examples with Model Technology's `vcom` compiler.

In order to load the memory initialization file (`*.mif`), it is required to be familiar with the programming language interface (PLI) of the Verilog 1364-1995 IEEE standard (see LRM Sect. 17, p. 228 ff.). With this powerful PLI interface, conventional C programs can be dynamically loaded into the Verilog compiler. In order to generate a dynamically loaded object from the program `convert_hex2ver.c`, the path for the include files `veriuser.h` and `acc_user.h` must be specified. Use `-I` when using the `gcc` or `cc` compiler under SUN Solaris. Using, for instance, the `gcc` compiler under SUN Solaris for the Model Technology Compiler, the following commands are used to produce the shared object:

```
gcc -c -I/<install_dir>/modeltech/include convert_hex2ver.c
ld -G -B symbolic -o convert_hex2ver.sl convert_hex2ver.o
```

By doing so, `ld` will generate a warning “Symbol referencing errors,” because all symbols are first resolved within the shared library at link time, but these warnings can be ignored.

It is then possible to use these shared objects, for instance, with Model Technology's `vsim` in the first design example `fun_text.v`, with

```
vsim -pli convert_hex2ver1.sl lpm.fun_text
```

To learn more about PLIs, check out the Verilog IEEE standard 1364-1995, or the vendor's user manual of your Verilog compiler.

We can use the script `mti_v1.do` to compile all Verilog examples with MTI's `vlog`. Just type

```
do mti_v1.do
```

in the ModelTech command line. But `vlog` does not perform a check of the correct component port instantiations or shared objects. A second script, `mti_v2.do`, can be used for this purpose. Start the `vsim` simulator (without loading a design) and execute the `DO` file with

```
do mti_v2.do
```

to perform the check for all designs.

**Using Xilinx ISE** The conversion of designs from Altera Quartus II to Xilinx ISE seems to be easy if we use standard HDL. Unfortunately there are a couple of issues that need to be addressed. We assume that the ModelTech simulation environment and the web version (i.e., no core generation) is used. We like to discuss in the following a couple of items that address the ISE/ModelTech design entry. We describe the Xilinx ISE 6.2 web edition and ModelTech 5.7g version.

- 1) The Xilinx simulation with timing ("Post-Place & Route") uses a bitwise simulation model on the LUT level. Back annotations are only done for the I/O ports, and are ALL from type `standard_logic` or `standard_logic_vector`. In order to match the behavior and the simulation with timing we therefore need to use only the `standard_logic` or `standard_logic_vector` data type for I/O. As a consequence no integers, generic, or custom I/O data type, (e.g., like the subtype byte see `cordic.vhd`) can be used.
- 2) The ISE software supports the development of testbenches with the "Test Bench Waveform." Use `New Source...` under the `Project` menu. This waveform will give you a quick way to generate a testbench that is used by ModelTech, both for behavior as well as simulation with timing. There are some benefits and drawbacks with the testbencher. For instance, you can not assign negative integers in the waveforms, you need to build the two's complement, i.e., equivalent unsigned number by hand.
- 3) If you have feedback, you need to initialize the register to zero in your HDL code. You can not do this with the testbencher: for instance, ModelTech initializes all integer signals to the smallest value, i.e.,  $-128$  for a 8-bit number, if you add two integers, the result will be  $-128 - 128 = -256 < -128$  and ModelTech will stop and report an overflow. Some designs, e.g., `cordic`, `cic3r32`, `cic3s32`, only work correctly in behavior simulation if all integers are changed to `standard_logic_vector` data type. Changing I/O ports alone and using the conversion function does not always guarantee correct simulation results.
- 4) Simulation with timing usually needs one clock cycle more than behavior code until all logic is settled. The input stimuli should therefore be zero in the first clock cycle (ca. 100 ns) and, if you want to match behavior and timing simulation, and the design uses a (small) FSM for control, you need to add a synchronous or asynchronous reset. You need to do this for the following 2/e designs: `dafsm`, `dadrom`, `dasign`, `db4latti`, `db4poly`, `div_aegp`, `div_res`, `iir_par`, `mul_ser`, `rader7`.

Just add a control part for the FSM like this:

```

-- IF rising_edge(clk) THEN          -- Synchronous reset
--   IF reset = '1' THEN
--     state <= s0;
--   ELSE
--     IF reset = '1' THEN           -- Asynchronous reset
--       state <= s0;
--     ELSIF rising_edge(clk) THEN
--       CASE state IS
--         WHEN s0 =>                 -- Initialization step
-- ...

```

Although at first glance this synchronous or asynchronous control seems to be cheap because the FSM is small, we need to keep in mind that, if the `reset` is active, all signals that are assigned in the state `s0` of the FSM need to be preserved with their initial state value. The following table shows the synthesis results for the three different reset styles for the design file `dafsm.vhd` (small distribute arithmetic state machine):

Reset style	Performance/ns	4-input LUT	Gates
No reset (original code)	3.542	20	339
synchronous	3.287	29	393
asynchronous	3.554	29	393

Designs with reset usually have a higher LUT and gate count. Depending on the design, synchronous or asynchronous reset can also have a (small) influence on performance.

- 5) Back annotation is only done for I/O ports. If we want to monitor internal nets, we can try to find the appropriate net name in the `*_timesim.vhd` file, but that is quite complicated and may change in the next compiler run. A better idea is to introduce additional test outputs, see, for instance, `fir_lms.vhd` for `f1_out` and `f2_out`. In the behavioral (but not in the timing) simulation internal test signals and variables can be monitored. Modify the `*.udo` file and add, for instance for the `fir_srg_tb.vhd` file, `add wave /fir_srg_tb/uut/tap` to the testbench.
- 3) There are a couple of nice features in the Xilinx ISE package too: there is no need for special `1pm` blocks to use the internal resources for multiplier, shifter, RAMs or ROMs. Some other features are:
  - a) ISE converts a shift register in a single CLB-based shift register. This can save some resources.
  - b) Multipliers can be implemented with LUTs only, including block multipliers (if available) or even pipelined LUTs, which is done via pipeline retiming. Just right click on the `Synthesize-XST` menu in the `Processes`, select `HDL Options` under `Process Properties` and the last entry is the multiplier style. But note that for pipelined LUT design the additional register must be placed at the *output* of the multiplier. Pipeline retiming is not done if the additional registers are at the inputs. You need about  $\log_2(B)$  additional registers to have good timing (see Chap. 2 on pipeline multiplier). This has an impact on the `Registered Performance`, LUT usage, and gates as the following table shows for the `fir_gen.vhd` example, i.e., length 4 programmable FIR filter (from Chap. 3):

Synthesis style	Speed in ns	4-input LUT	mul. blocks	Gates
Block multiplier	9.838	57	4	17552
LUT (no pipeline)	15.341	433	0	6114
LUT (3 stage pipeline)	6.762	448	0	9748

For this multiplier size (9 bit) the pipelined LUT seems to be attractive, both for speed as well as gate count. If the number of LUTs is limited, the block multiplier provides the next best alternative.

- c) If you follow the recommended style the Xilinx software synthesis tool (see XST manual and ISE help “Inferring BlockRAM in VHDL”) maps your HDL code to the block RAM (see, `fun_text.vhd`). If the table is small, the ISE auto option selects the LUT-based implementation for a ROM table (see `darom.vhd`). You can also initialize the table in the HDL code and use it as a ROM. Please see the XST manual Chap. 3, “FPGA Optimization” for details on ROM implementation. There are some limitations that apply to the initialization of BlockRAMs (see, XST Chap. 2)

## Utility Programs and Files

A couple of extra utility programs are also included on the CD-ROM<sup>1</sup> and can be found in the directory `book3e/util`:

File	Description
<code>sine3e.exe</code>	Program to generate the MIF files for the function generator in Chap. 1
<code>csd3e.exe</code>	Program to find the canonical signed digit representation of integers or fractions as used in Chap. 2
<code>fpinv3e.exe</code>	Program to compute the floating-point tables for reciprocals as used in Chap. 2
<code>dagen.exe</code>	Program to generate the VHDL code for the distributed arithmetic files used in Chap. 3
<code>ragopt.exe</code>	Program to compute the reduced adder graph for constant-coefficient filters as used in Chap. 3. It has 10 predefined lowpass and half-band filters. The program uses a MAG cost table stored in the file <code>mag14.dat</code>
<code>cic.exe</code>	Program to compute the parameters for a CIC filter as used in Chap. 5

The programs are compiled using the author’s MS Visual C++ standard edition software (available for \$50–100 at all major retailers) for DOS window applications and should therefore run on Windows 95 or higher. The DOS script `Testall.bat` produces the examples used in the book.

Also under `book3e/util` we find the following utility files:

---

<sup>1</sup> You need to copy the programs to your harddrive first; you can not start them from the CD directly since the program write out the results in text files.

File	Description
<code>quickver.pdf</code>	Quick reference card for Verilog HDL from QUALIS
<code>quickvhd.pdf</code>	Quick reference card for VHDL from QUALIS
<code>quicklog.pdf</code>	Quick reference card for the IEEE 1164 logic package from QUALIS
<code>93vhdl.vhd</code>	The IEEE VHDL 1076-1993 keywords
<code>95key.v</code>	The IEEE Verilog 1364-1995 keywords
<code>01key.v</code>	The IEEE Verilog 1364-2001 keywords
<code>95direct.v</code>	The IEEE Verilog 1364-1995 compiler directives
<code>95tasks.v</code>	The IEEE Verilog 1364-1995 system tasks and functions

In addition, the CD-ROM includes a collection of useful Internet links (see file `dsp4fpga.htm` under `book3e/util`), such as device vendors, software tools, VHDL and Verilog resources, and links to online available HDL introductions, e.g., the “Verilog Handbook” by Dr. D. Hyde and “The VHDL Handbook Cookbook” by Dr. P. Ashenden.

## Micropocessor Project Files and Programs

All microprocessor-related tools and documents can be found in the `book3e/uP` folder. Six software Flex/Bison projects along with their compiler scripts are included:

- `build1.bat` and `simple.l` are used for a simple Flex example.
- `build2.bat`, `d_ff.vhd`, and `vhdlcheck.l` are a basic VHDL lexical analysis.
- `build3.bat`, `asm2mif.l`, and `add2.txt` are used for a simple Flex example.
- `build4.bat`, `add2.y`, and `add2.txt` are used for a simple Bison example.
- `build5.bat`, `calc.l`, `calc.y` and `calc.txt` is an infix calculator and are used to demonstrate the Bison/Flex communication.
- `build6.bat`, `c2asm.h`, `c2asm.h`, `c2asm.c`, `lc2asm.c`, `yc2asm.c` and `factorial.c` are used for a C-to-assembler compiler for a stack computer.

The `*.txt` files are used as input files for the programs. The `buildx.bat` can be used to compile each project separately; alternatively you can use the `uPrunall.bat` under Unix to compile and run all files in one step. The compiled files that run under SunOS UNIX end with `*.exe` while the DOS programs end with `*.com`.

Here is a short description of the other supporting files in the `book3e/uP` directory: `Bison.pdf` contains the Bison compiler, i.e., the YACC-compatible parser generator, written by Charles Donnelly and Richard Stallman; `Flex.pdf` is the description of the fast scanner generator written by Vern Paxson.

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